



Robert Millikan (top center) on the steps of Ryerson Laboratory, U. of Chicago, 1908. Other colleagues (L-R): A. A. Michelson, Carl Kinsey, Henry G. Gale

## ROBERT A. MILLIKAN

### Oil Drop Experiment Notebooks

NOTEBOOK ONE:  
October 1911-March 1912

PART 3 OF 3  
From page 80 to page 124

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### Abstract

Robert A. Millikan (1868-1953) began his experiments to measure the charge on the electron,  $e$ , in 1907. The experiments were performed in Ryerson Laboratory at the University of Chicago, where Millikan was professor of physics. For this work, and for work on the photoelectric effect, Millikan was awarded the Nobel Prize in physics in 1923.

Millikan gives his own account of the electron charge determination in his published autobiography in the chapter titled "My Oil-Drop Venture ( $e$ )" (Robert A. Millikan, *The Autobiography of Robert A. Millikan*, New York, 1950). With the aid of graduate students Louis Begeman, Harvey Fletcher, and J. Y. Lee, Millikan devised the method of measuring the rate of fall of a single electrically charged oil drop under the forces of gravity and electricity. From 1909 until the spring of 1912, Millikan reports, he spent every available moment in the laboratory on his oil-drop experiment. His first comprehensive, though to some extent preliminary, results were published in September 1910 in the journal *Science* as "The Isolation of an Ion, a Precision Measurement of Its Charge, and the Correction of Stokes' Law," *Science* 32: 436-448. He soon became embroiled in a controversy with the Viennese physicist Felix Ehrenhaft, who claimed to have found much smaller electric charges. Millikan went back to work on a new

set of experiments. By the spring of 1912 he had collected the data for what he termed “the final, absolute determination of the numerical value of the electron” (*Autobiography*, p. 84). Results were published in August 1913 in “On the Elementary Electrical Charge and the Avogadro Constant,” *Physical Review* 2: 109-43. This last, definitive set of experiments were recorded in the only two lab notebooks which Millikan preserved among his papers. These two notebooks are presented here in facsimile. They cover the period from October 1911 through April 1912 and contain what Millikan himself considered his conclusive, historic work on this problem.

For an analysis of Millikan’s notebooks and a defense of his experimental method, see the article by David Goodstein, “In Defense of Robert Andrews Millikan,” published in *American Scientist* 89/1 (Jan-Feb. 2001): 54.

<http://www.americanscientist.org/issues/num2/2001/1/in-defense-of-robert-andrews-millikan/1>

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### **Preferred citation**

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### **Contact information**

Archives, California Institute of Technology  
Mail Code 015A-74  
Pasadena, CA 91125  
Phone: (626) 395-2704 Fax: (626) 793-8756  
Email: [archives@caltech.edu](mailto:archives@caltech.edu)

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Friday - Feb. 16, 1912

$$A = 23.0$$

$$P = 28.0$$

Valt at 4:05 PM

$$848 + 12.7$$

$$842 + 13.1$$

$$824 + 14.5$$

$$855 + 12.8$$

$$827 + 14.3$$

$$841 + 13.2$$

$$5037 + 80.8 = 5117.8$$

Y		F	
21.4	59.3	<del>22.8</del>	22.8
29.0	59.4		23.0
29.0	59.8		
	59.8		

# Second Observation.

$$A = 33.00$$

$$P = 28.88$$

29

Volts at 5:10

$$848 + 12.9$$

$$839 + 13.2$$

$$821 + 14.8$$

$$854 + 12.8$$

$$826 + 14.5$$

$$840 + 13.2$$

$$5028 + 71.4 = 5099.4$$

G	F
12.2 24.0	
12.3 24.0	
11.9 24.0	
24.170	10.354
24.914	
24.114	12.444
24.280	
24.108	
	22.138
	51.3—
24.108	
24.086	18.0— 35.7—
24.008	62.6— 1 <sup>st</sup> div.
	60.7— 2 <sup>nd</sup> div.
	63.9— 3 <sup>rd</sup> div.
	57.8— 4 <sup>th</sup> div.
	60.0— 5 <sup>th</sup> div.
	58.7— 6 <sup>th</sup> div.
	58.8— 7 <sup>th</sup> div.
	59.6— 8 <sup>th</sup> div.
24.310	
24.386	<del>25.34</del>
	34.334
	46.00 42.20

Finished at 5:05

25

Saturday, Feb. 17<sup>th</sup> 1912

$\theta = 23.0$

$$p = \frac{75.75}{41.63} = 34.10$$

Observation at 3:00 P.M.

Volts at 2145

S		F	
16.6	32.6		
16.3	32.7		
16.0	32.9	47.6	94.4
16.6	33.2		
Lost at 3:07			

$856 + 12.8$

$848 + 12.9$

$840 + 13.2$

$862 + 12.8$

$840 + 13.2$

$848 + 12.9$

$5094 + 77.8 = 5171.8$



Second Observation at 3:20

$$\theta = 23.0$$

$$p = 36.17 \sim 36.04$$

Volts at 3:10

$$856 + 12.8$$

$$848 + 12.9$$

$$839 + 13.2$$

$$862 + 12.8$$

$$839 + 13.2$$

$$847 + 12.9$$

$$5091 + 17.8 = 5168.8$$

G.		F
10.418		99.12
10.464		9.988
10.438		9.956
10.342		9.508(?)
10.422		
10.470	23.7-	46.8-
10.414		
10.402	47.6	94.4
10.412		15.702
10.476		17.624
	18.9	37.8-
	31.7	62.6-
	31.6	62.6-
10.430		23.106
10.500		23.302
	11.9	23.7-
	32.0	63.4-
		63.2-
	48.4	95.8

Finished at 3:45

Thick Obs. at 4:00

$$\theta = 23.0$$

$$p = \frac{7695}{40.50} = \frac{7705}{40.10} = 3675$$

Volto at 3:50 -

$$\begin{array}{r} 856 + 12.8 \\ 847 + 12.9 \\ 837 + 13.4 \\ 861 + 12.8 \\ 835 + 13.6 \\ 847 + 13.0 \end{array}$$

$$508.6 + 78.5 = 587.1$$

Differences

$$\begin{array}{r} .07331 \\ .02793 \\ \hline .04538 \\ 6 \overline{) .04538} \\ .007397 \end{array}$$

Agreement prev. Millikan

$$\begin{array}{r} 4409 \\ 7331 \\ \hline 16 \overline{) .12240} \\ .00765 \end{array} \quad \begin{array}{r} 2008 \\ 4909 \\ 2793 \\ \hline 107702 \\ .007702 \end{array} \quad \begin{array}{r} 4409 \\ 1266 \\ 4909 \\ \hline 969175 \\ .007686 \end{array} \quad \begin{array}{r} 4409 \\ 4409 \\ 1266 \\ \hline 61757 \\ 7719, 7715 \end{array}$$

$$\text{mean } .007695$$

G	F
20.362	13.678
20.418	13.590
20.380	
10.2 - 20.3 -	18.3 - 35.8 -
20.394	25.2 - 49.8 -
20.442	39.9 - 79.0 -
20.340	102.2 - 202.8 -
20.358	101.6 - 203.0 -
20.324	
91.3318	
20.369	
$\frac{1}{20.37} = .04909$	

Found  $\phi$  at 5.15

$$\theta = 23.$$

$$p = \frac{65.45}{50.20} = 1.303$$

Voltage 4.23

$$\begin{aligned} 854 + 12.8 \\ 847 + 12.9 \\ 835 + 13.6 \\ 860 + 12.8 \\ 833 + 13.4 \\ 845 + 13.0 \end{aligned}$$

$$3074 + 78.5 = 3152.5$$

Pressure at 5.15-18.25  
5.28-18.45  
5.35-18.45

G

F

14.456	64.0	127.0
14.464		23.296
14.522		23.300
14.522		23.206
14.522		23.310
14.568	11.6	23.2
14.540	23.4	45.6
14.466	33.6	67.1
14.548	33.4	66.6
14.514	33.6	66.4
<del>14.364</del>	17.6	34.7
14.470	17.0	34.24

$$\frac{1}{127} = .007874$$

$$\frac{1}{23.28} = .04296$$

$$\frac{1}{45.6} = .02193$$

$$\frac{1}{66.7} = .01499$$

$$\frac{1}{34.7} = .02882$$

Finished at 5.32

14.509

$$\frac{1}{14.509} \cdot .068925 \times 1022 = .07044$$

$$\log -2.847819$$

$$\frac{1}{2} \log = -1.4239$$

Differences

$$\begin{array}{r} .04296 \quad .04296 \quad 4296 \quad 2807 \\ .007874 \quad 2193 \quad 1499 \quad 7499 \\ 5) .0350863 \quad .02103 \quad 4 \quad 27972 \quad 1408 \\ .07017 \quad .07010 \quad .06993 \quad 7016 \end{array}$$

$$\begin{array}{r} .068925 \quad 68925 \quad 68925 \quad 68925 \quad 68925 \\ 7874 \quad 4296 \quad 2193 \quad 1499 \quad 7499 \\ 11) .076799 \quad 10 \quad 111945 \quad 11 \quad 90855 \quad 462912 \quad 42100 \\ .068981 \quad .06999 \quad 6989 \quad 6993 \quad 7016 \end{array}$$

$$\text{mean} = .06996 \times 1022$$

$$v_1 + v_2 = .07150$$

$$\log = 3.854306$$

$$\begin{array}{r} 1.42391 \\ 3.1983 \\ 6.476516 \\ 3.712229 \\ 10.764289 \end{array}$$

Voltage 5.155

$$e_1 = 5.8113$$



7th Obs.

at 5:40

$\theta = 23.2$

$P = \frac{6879}{4974} = 1.382$

at 5:57  
 $\frac{6879}{4974} = 1.382$   
 $\frac{6885}{4975} = 1.385$

Volts at 6:20

G	F
17.132	23.2
17.382	23.0
17.320	23.100 $\frac{1}{23.1} = 0.04329$
17.346	22.9
	27.4 1st div.
	2nd div.
	3rd div.
	28.1 4th div.
	27.0 5th div.
	28.0 6th div.
	28.6 7th div.
	8th div.
17.324	27.6 1st div.
5/160.4	28.2 2nd div.
17.321	28.2 3rd div.
	28.4 4th div.
	27.9 5th div.
	28.1 6th div.
	27.8 7th div.
	27.4 8th div.
	223.6

$$\frac{1}{17321} = 0.5773 \times 10^{-2}$$

$$= v_1 = 0.5773$$

$$L_1 = -2.77085 \text{ v}$$

$$\frac{1}{v_1} = -1.38542$$

$$= v_1 = 0.5773$$

$$\begin{aligned} 849 + 12.9 \\ 838 + 13.4 \\ 823 + 14.5 \\ 853 + 12.8 \\ 823 + 14.7 \\ 840 + 13.2 \end{aligned}$$

$$5028 + 81.5 = 5109.5$$

offs

$$\begin{aligned} .04329 \\ 004484 \\ 5 \overline{) 038806} \\ 007761 \end{aligned}$$

$$\begin{aligned} .05773 \\ 004484 \\ 8 \overline{) 062214} \\ 007777 \end{aligned}$$

$$\begin{aligned} .05773 \\ 04329 \\ 8 \overline{) .10102} \\ .107771 \end{aligned}$$

$$\text{mean} = 0.07774 \times 10^{-2}$$

$$= v_1 + v_2 = 0.07945$$

$$\begin{aligned} L_2 &= -3.90094 \\ &-1.38542 \\ &-3.1983 \\ &-6.4838 \\ &3.7084 \\ &-10.7754 \end{aligned}$$

$$5962$$

$$e_1 = 5966$$

Don Pinner

Beginning with Oil bath - not entirely covered with oil.

Friday - Feb. 23<sup>rd</sup> 1912.  
Obs. began at 4:50 P.M.

$$\theta = 23.2 \quad P = 44.3 - 19.4 = 74.9$$

Volts at 5:30

G		F	
21.4	42.6	33.8	68.4
21.3	42.9	58.3	117.4
21.6	43.1	24.3	47.7
22.0	43.3	34.0	67.3
21.0	42.8	23.6	47.2
21.6	42.9	18.0	36.2
21.4	43.4	24.0	47.5
21.0	42.7	—	36.0
21.6	43.2	23.6	47.0
91269			
42.98			

$$\frac{1}{42.98} = 0.2327 \times 1022 = 0.2378$$

$$\text{Log} = -2.376212$$

$$\frac{1}{2}11 = -1.18811$$

Finished at 5:25 P.M.

$$\begin{aligned} 1-7.35+18.0 \\ 2-8.57+12.8 \\ 3-8.48+12.9 \\ 4-5.22+06.0 \\ \hline 29.62+49.7 = 3011.7 \end{aligned}$$

Differences

$$\begin{array}{r} .81413 \\ .00639 \\ \hline .82052 \end{array} \quad \begin{array}{r} .02113 \\ .008518 \\ \hline .029648 \end{array} \quad \begin{array}{r} 2770 \\ 8578 \\ \hline 36278 \end{array}$$

$$\text{mean} = 0.06363$$

$$\begin{array}{r} .02327 \\ .01474 \\ \hline .03801 \end{array} \quad \begin{array}{r} .02327 \\ .02113 \\ \hline .04440 \end{array} \quad \begin{array}{r} .02327 \\ 2770 \\ \hline 30497 \end{array} \quad \begin{array}{r} 2327 \\ 8578 \\ \hline 10905 \end{array}$$

$$\begin{array}{r} 6 \quad .038017 \\ \hline .006335 \end{array} \quad \begin{array}{r} .04440 \\ \hline .006343 \end{array} \quad \begin{array}{r} .050973 \\ \hline .006375 \end{array} \quad \begin{array}{r} 10905 \\ \hline .006362 \end{array}$$

$$\text{mean} = .006354 \times 1022$$

$$= v_1 + v_2 = .006444$$

$$\text{Log} = -3.812512$$

$$\begin{array}{r} -1.18811 \\ 2.1963 \\ \hline 6.198922 \\ 3.47881 \\ \hline 70.72011 \end{array}$$

$$\begin{array}{r} 5.2495 \\ 70 \\ \hline \end{array}$$

$$e_1 = 5.2565 \quad \text{Correct} = 5.310$$

1.0 % low

Saturday Feb. 24<sup>th</sup> 1912

[1067 middle  
7 plates]

First Obs at 3:15  $\theta = 23.5$

$p = 94.45 - 19.5 = 75.30$

Valts at 3:05 -  $858 + 12.8$

$856 + 12.8$

$848 + 12.9$

$863 + 12.8$

$836 + 13.6$

$851 + 12.9$

$5112 + 77.5 = 5189.8$

Differences

.03195	.03856	.03856	.02551
.02558	.02558	.01922	.01922
.00639	.01398	.01924	.00629

.06490 .006413

mean = .006398

.06375	.6375	.6375	.6375
.3195	.555	.3661	.192
10) .09570	14) 8930	16) 10236	13) 4297
.006380	.006379	.006394	.006382

mean = .006384  $\times 1.022$

$= v_1 + v_2 = .0065244$

$\log v_1 + v_2 = -3.814541$

$= -1.406957$

$\frac{1}{2} v_1 = -3.1985$

$-6.419798$

$3.714414$

$10.705384$

mean with 5181

50743

115 correct = 5138

5086

1.09 low

G

F

15.750

15.712

15.748

15.626

15.680

15.564

15.716

15.666

15.712

15.676

10) 68.50

15.686

$\frac{1}{15.686} = .06375$

$\times 1.022 = .06515$

$\log = -2.612914$

$\frac{1}{2} v_1 = -1.406957$

8.750

31.4 -  $\frac{1}{21.3} = .03195$

31.2 -  $\frac{1}{39.1} = .02558$

15.6 39.2 -  $\frac{1}{39.1} = .02558$

19.6 39.0 -  $\frac{1}{25.87} = .03856$

19.9 39.0 -  $\frac{1}{25.87} = .03856$

12.9 25.6 -  $\frac{1}{52.02} = .01922$

12.9 26.0 -  $\frac{1}{52.02} = .01922$

13.0 26.0 -  $\frac{1}{52.02} = .01922$

26.4 52.2 -  $\frac{1}{52.02} = .01922$

26.0 51.8 -  $\frac{1}{52.02} = .01922$

26.3 52.2 -  $\frac{1}{52.02} = .01922$

26.3 52.0 -  $\frac{1}{52.02} = .01922$

26.2 51.9 -  $\frac{1}{39.2} = .02551$

39.2  $\frac{1}{39.2} = .02551$

mean at 3:45



# Second Observation

$\theta = 23.7$   
Voltage 3:55

$P_2 = 9430 - 19.25 = 76.05$

4:05

857 + 12.8  
855 + 12.8  
843 + 13.1  
862 + 12.8  
832 + 13.8  
849 + 12.9

5098 + 78.2 = 5176.2

Difference

03924  
02270  
01654

01070 01070  
03924 02270  
3) 04999 2) 03340  
01666 01670

mean = 01667 x 1022

$V_1 + V_2 = 01693$

$V_1 =$

$\log V_1 + V_2 = -2.22866$

$\frac{1}{2} V_1 = -1.01941$

-31483

-6.44637

3.71332

-10.73305

mean value 5166

5.408

19

Corrected to  $(\frac{d}{100}) = 5.417$

5.425

Corrected = 5.446

$\lambda = 0.0004570$

1.5 % low

Cf with Lawrence  
Feb 13/47

-6.4805

-5.4835

2.9970

0.09933 =  $\frac{1}{a}$

$e^{V_1}$

3) -10.7338

-4.9913

-7.8226

66.47 =  $e^{V_2}$

G	F
11.6 - 1 <sup>st</sup> div	
11.4 - 2 <sup>nd</sup> div	
11.9 - 3 <sup>rd</sup> div	
11.7 - 4 <sup>th</sup> div	
11.8 - 5 <sup>th</sup> div	
11.5 - 6 <sup>th</sup> div	
11.4 - 7 <sup>th</sup> div	
11.3 - 8 <sup>th</sup> div	
93.6	

11.9 - 1<sup>st</sup> div  
11.7 - 2<sup>nd</sup> div  
12.0 - 3<sup>rd</sup> div  
11.0 - 4<sup>th</sup> div  
11.4 - 5<sup>th</sup> div  
11.6 - 6<sup>th</sup> div  
12.0 - 7<sup>th</sup> div  
11.6 - 8<sup>th</sup> div  
93.2

25.2 \*

$\frac{1}{44.018} = 0.02270$   
44.06

23.6 - (1+2)  
23.4 - (3+4)  
23.6 - (5+6)  
23.0 - (7+8)  
93.6

25.452  $\frac{1}{25.45} = 0.03924$

44.094

47.0 - 93.5  
93.8

mean = 93.52

Finished at 4:28

$\frac{1}{93.52} = 0.01070 \times 1022 = 0.010933$

$\log = -2.03882$

$\frac{1}{2} V_1 = -1.01941$

Sum a  
-16.4270  
+3.7133  
-2.0388  
-14.1711  
-2.2287  
3) -13.9504  
-5.4835  
1.8754  
-3.6569  
2.1415

0.0009628 = a

138.40 =  $\frac{1}{a}$



3<sup>rd</sup> Third Observation -

(No 1)

4:40

$\theta = 23.7$

Volts at 4:30

$p = 9435 - 19.15 = 75.20$

G	F	F
124 - 250		
25.486	23.6	$\frac{1}{23.6} = .04237$
25.354	19.824	$\frac{1}{19.83} = .05043$
25.376	28.4 - 56.6	$\frac{1}{56.55} = .017685$
25.350	28.4 - 56.5	
25.348	52.4 - 104.0	$\frac{1}{104} = .009615$
25.358		
65302		
25.384		

$$\frac{1}{25.384} = .039348 \times 10^5 = .040263 = V_1$$

$$\log = -2.604907$$

$$\frac{1}{2} = -1.30245$$

Finished at 4:55

$e\%$

$a$

$$3) 20.7102 - 30$$

$$6.9354 - 10$$

$$13.8068 - 10$$

$$11.6409 - 10^8$$

$$16.4270$$

$$3.71315$$

$$2.60491$$

$$74.74506$$

$$-3.92128$$

$$3) 12.83378$$

$$7.27459$$

$$1.67623$$

$$a = .0001882$$

$$\log a = 2.1508$$

$$\log a = 1.8492$$

$$\frac{1}{a} = 7.067$$

$$856 + 12.4$$

$$854 + 12.8$$

$$83.8 + 13.3$$

$$861 + 12.8$$

$$830 + 14.1$$

$$849 + 12.9$$

$$5088 + 78.7 = 5166.7$$

$$\text{Differences } .017685 \quad .05043$$

$$.017685 \quad .017685$$

$$.008070 \quad 4) 0.32745$$

$$.008086$$

$$.020885 \div .008228 \quad \text{mean} = .008128$$

$$.039396 \quad .039396 \quad .039396$$

$$.5093 \quad .017685 \quad .615$$

$$11) .089826 \quad 7) .057083 \quad 6) .049010$$

$$.008166 \quad .008154 \quad .008168$$

$$\text{mean} = .008164 \times 10^2 = .0083428$$

$$\log = -3.921286$$

$$\frac{1}{2} = -1.30245$$

$$-3.1983$$

$$-6.422036$$

$$71315$$

$$70888$$

$$51155$$

$$158$$

$$e_1 = 51313 \quad \text{Correct} = 5.206$$

$$e_1 = 5.124 \quad \text{Chrom. Corr.}$$

$$1.46\% \text{ Loss}$$

$$-4.8517$$

$$1.8762$$

$$-6.9785$$

$$-4.2746$$

$$2.7039$$

$$\frac{1}{a} = 0.5067$$

$$\mu a = .01415$$

2  
48

Fourth Observation

$\theta = 23.5$   $p = 94.4 - 19.1553$

Volts at 4:56

856 + 12.8  
854 + 12.8  
837 + 13.0  
861 + 12.0  
830 + 14.1  
848 + 12.9

5086 + 74.0 = 5160.8

G	F
12.572	49.0 - 97.1 -
12.522	31.7 - 62.9 -
12.578	31.4 - 62.8 -
	27.6 - 13 div.
	27.4 - 25 "
	27.4 - 25 "
	27.2 - 40 "
	26.4 - 50 "
	27.3 - 60 "
	26.1 - 70 "
12.574	25.2 - 80 "
	214.6
12.420	36.6
	37.0
12.594	36.8
12.544	18.5 - 37.0
12.562	
12.510	63.0
12.514	
10/5400	
12.54	

$\frac{1}{97.1} = .01030$  Beauty

$\frac{1}{62.85} = .01591$

Volts at 3:30

856 + 12.8  
853 + 12.0  
836 + 13.0  
860 + 12.0  
828 + 14.3  
848 + 12.9

5081 + 78.2 = 5159.2

$\frac{1}{214.6} = .004660$

Differences.

.01591 .01591 .027135 .027135  
.01030 .00466 .00466 .01591  
.00561 2/01125 4/022475 4/01125  
0562 .005619 5642

mean = .0056225

.07974 .07974 .07974  
.01030 .1591 466  
16/ .09004 109565 109565  
05627 05625 05627

.07974 7974 5027  
27135 1585 5625  
14/106875 179559 5625  
05625 5623 5623

.0056244

$V_1 + V_2 = \text{mean} = .005623 \times 1022 = .0057467$

$\log = -3.75908$

$-1.45538$

$-3.1962$

$6.41265$

$3.71285$

$-10.7000$

$5.5474$

$50120$

$1.03527$

$3844$

$5.023$

$1.00208$

$1.57\% \text{ slow}$

$e\%$   
 $3/-10.7019$   
 $6.9006 - 10.1400$   
 $13.8012 - 20.0000$   
 $63.27 \times 10 = e\%$

uncert = 5.113 Error 2%

$1.57\% \text{ slow}$

$\frac{2}{-16.4270}$   
 $\frac{3}{3.7128}$   
 $\frac{4}{-2.9106}$   
 $\frac{5}{-13.0509}$   
 $\frac{6}{3.75940}$   
 $\frac{7}{3/-11.2915}$   
 $\frac{8}{4.4305}$   
 $\log A = 1.8768$   
 $\frac{9}{2.3073}$   
 $\log L = 21.6927$   
 $\frac{10}{4920}$   
 $\frac{11}{4952}$

Publish the  
Brachistochrone  
problem for showing  
method of  
computation and  
how e can be made  
ind of m

Tuesday - Feb. 27<sup>th</sup> 1912  
 First Observation  
 Began at 3:10 P.M.

$$\theta = 22.8 \quad p = 94.3 - 19.2 = 75.1$$

Volts at 2:50 P.M.

$$\begin{aligned}
 &855 + 12.8 \\
 &859 + 12.8 \\
 &841 + 13.2 \\
 &864 + 12.8 \\
 &838 + 13.4 \\
 &852 + 12.8
 \end{aligned}$$

$$\begin{aligned}
 \frac{1}{58.6} &= 0.01706 \times 1021 = 0.017162 = 510.9 + 77.9 = 5186.9 \\
 \frac{1}{29.3} &= 0.03413 \\
 \frac{1}{0.5119 \times 1021} &= 0.052265 = v_1 + v_2 = 45.00009
 \end{aligned}$$

Finished at 3:14 P.M.

This one is not  
 yet placed on  
 acid form P.H.O.

$$\begin{aligned}
 &\log -2.71821 \\
 &-1.11755 \\
 &\hline
 &3.1983 \\
 &-5.03406 \\
 &\hline
 &3.7120 \\
 &4) 20.992 \\
 &\quad 5.248 \\
 &\quad \hline
 &\quad 5.243
 \end{aligned}$$

$$\log -2.1161$$

$$e, \quad 5.243 \quad 5.375 = \text{const}$$

$$2.5\% \text{ error}$$

lower 12

$$\begin{aligned}
 &16.4270 \\
 &3.7120 \\
 &-2.1351 \\
 &\hline
 &14.3741 \\
 &-2.1161 \\
 &\hline
 &3) 12.2580
 \end{aligned}$$

$$\begin{aligned}
 &-4.0860 \cdot 0.001219 = a \\
 &1.8756 \cdot 0.004154 = pa \\
 &12.0384 \quad 109.2 = \frac{1}{pa}
 \end{aligned}$$

$$k = 0.00000953$$

$$\begin{aligned}
 &-4.85474 \\
 &1.8756 \\
 &-6.97914 \\
 &-4.0860 \\
 &\hline
 &-2.84314
 \end{aligned}$$

$$0.7818 = \frac{1}{a}$$

$$\begin{aligned}
 &31-6.7145 \\
 &6.9065 - 10 \\
 &\hline
 &13.8130 - 30
 \end{aligned}$$

$$\begin{aligned}
 &81.30 \dots \dots e^{1/3} \\
 &65.02 =
 \end{aligned}$$

$$\begin{aligned}
 &4.8547 \\
 &1.8756 \\
 &6.9791 \\
 &-4.4634 \\
 &\hline
 &-2.5157 \\
 &\frac{1}{a} = 0.03278
 \end{aligned}$$

$$\begin{aligned}
 &-16.4270 \\
 &3.7118 \\
 &-2.9712 \\
 &\hline
 &-13.1160 \\
 &-3.7259 \\
 &\hline
 &3) -11.3903 \\
 &\quad -6.4634 - 10 \\
 &\quad \hline
 &\quad -4.9269
 \end{aligned}$$

$$\begin{aligned}
 &-2.3390 = \log pa \\
 &.02183 = pa \\
 &1.6610 \\
 &45.61 = \frac{1}{pa}
 \end{aligned}$$

$$\begin{aligned}
 &31-10.7008 \\
 &6.9003 - 10 \\
 &\hline
 &-7.6006 \\
 &63.19 = e^{1/3}
 \end{aligned}$$



$$p = 94.35 - 19.15 = 75.2$$

27

 $855 + 120$ 

mean volts  
5.52

$\mathcal{L} = 5.001$

413

1570  
1875  
Furnished at 4:26

$$\frac{1}{10358} = .09294 \times 1021 = .09469 =$$
$$Z_{0.9} = -1.47$$

[http://resolver.caltech.edu/CaltechLN:LN\\_Millika](http://resolver.caltech.edu/CaltechLN:LN_Millika)

fine

19.



70) Feb. 27 - 204  
Third Observation  
at 11:40

$$\theta = 22.87$$

$$p = 94.2 - 19.28 = 75.0$$

Volts at 4:27

$$\begin{aligned} 851.0 + 12.9 \\ 853.0 + 12.8 \\ 857.0 + 14.3 \\ 861.0 + 12.8 \\ 857.0 + 14.3 \\ 849.0 + 12.8 \\ \hline 5068.0 + 79.9 = 5147.9 \end{aligned}$$

G	F		
13.582	—	16.450	16.450 = .06079
13.588	—	20.458	
13.594	—	20.492	20.431 .04695
13.572	—	20.266	
13.544	63.6	126.0	
13.542	63.9	127.6	126.66 .007893
13.648	63.6	126.4	
13.582	—	27.010	26.932 .03713
13.536	—	26.854	
13.500			
13.580			
13.562			

Differences

$$\begin{array}{r} .04695 \quad .03713 \quad .03713 \quad .03713 \\ .00789 \quad .00789 \quad .00789 \quad .00789 \\ \hline .04106 \quad .01184 \quad .01184 \quad .01184 \\ \hline .005866 \quad .00592 \quad .005848 \quad .00591 \\ \hline \text{mean} = .005857 \end{array}$$

$$\begin{array}{r} .072746 \quad .073746 \quad .073746 \quad .073746 \\ .06079 \quad .04695 \quad .04695 \quad .04695 \\ \hline .01194536 \quad .026796 \quad .026796 \quad .026796 \\ \hline 5849 \quad 5842 \quad 5837 \quad 5835 \\ \hline \text{mean} = 5839.2 \end{array}$$

5:00 P.M.

$$\begin{aligned} \frac{1}{1356} &= .073746 \times 1021 = .075294 \\ \log &= -2.87676 \\ \frac{1}{10} &= -1.43842 \end{aligned}$$

$$\begin{aligned} x_1 + x_2 &= .0059618 \\ \log &= -3.77538 \\ &= -1.43838 \\ &= 3.1483 \\ &= 6.41206 \\ &= 3.71095 \\ \text{mean volts} &= 5139.5 \end{aligned}$$

a

$$\begin{array}{r} -16.4270 \\ 3.7108 \\ \hline -2.8768 \\ \hline -13.0146 \\ -3.7754 \\ \hline 3) -11.2392 \\ -4.4110 \\ \hline 1.5751 \\ -2.2583 \\ \hline 1.7138 \end{array}$$

0.000009542

$$\begin{array}{r} -4.5547 \\ 1.5751 \\ \hline -6.9790 \\ -4.4131 \\ \hline -2.5665 \end{array}$$

3702  
3697 = 1/2  
0.03666 = 1/2

0.0002569 = a  
2571  
5150 = 2570 ha

Compared for mean

$$9557985834 =$$

5022  
5021  
1.8% low  
C = 5016

5124 = constant  
Probly some 45%  
two low judged  
from diff bit  
5857 + 5839

7003  
2  
319006  
2  
73002  
63.13 = 2%

Feb. 27<sup>th</sup>

$A = 22.86$

$B = 94.2 - 19.2 = 75.0$

Fourth Observation  
at - 5:15

Volts at - 5:05

$$\begin{aligned}
 &850 + 12.9 \\
 &851 + 12.9 \\
 &820 + 14.8 \\
 &860 + 12.8 \\
 &827 + 14.3 \\
 &848 + 12.8 \\
 &5066 + 80.6 = 5136.6
 \end{aligned}$$

No 5

Harnessed

Diff. to correct  
V. justified  
in this case.

Perhaps, Peltier

Differences

$$\begin{array}{r}
 .1031 \quad 3400 \quad 3406 \quad 2994 \quad 3400 \\
 1416 \quad 1416 \quad 2444 \quad 6006 \quad 6006 \\
 25108894 \quad 501984 \quad 1004066 \quad 23924 \quad 727994 \\
 4043 \quad 3966 \quad 3989 \quad 3989 \quad 3989
 \end{array}$$

$$\begin{array}{r}
 1031 \quad 1553 \quad 1553 \\
 1553 \quad 1416 \quad 3400 \\
 64 \quad 2584 \quad 16946 \quad 15930 \\
 4037 \quad 4035 \quad 4028
 \end{array}$$

$$\begin{array}{r}
 1553 \quad 1553 \\
 2994 \quad 6006 \\
 46 \quad 18524 \quad 46 \quad 161304 \\
 4027 \quad 4032
 \end{array}$$

mean of  $4032 + 4000 = .004016 \times 10^{-1}$

$= V_1 + V_2 = .004100$  Take with four

$\log = -3.61278$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

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$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

6	F
6.354	9.756
6.394	9.776
6.468	9.572
6.402	35.6 70.6
6.388	35.6 70.8
6.448	85.2 70.4
6.492	35.6 70.5
6.424	70.8
6.454	29.416
6.438	29.384
6.420	29.440
6.430	33.2
6.492	33.388
6.494	33.460
	33.366
	84.0 166.5
6.504	166.6
6.446	

$\frac{1}{9.700} = .1031$

$\frac{1}{70.62} = .01416$

$\frac{1}{29.41} = .03400$

$\frac{1}{33.405} = .02994$

$\frac{1}{166.5} = .006004$

finished at 5:45

$\frac{1}{6.4} = .1553 \times 10^{-1} = V_1 = .15823$

$\log = -1.20019$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\log \text{ new } V_1 = 1.965$

$\frac{1}{2} = -1.5483$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$\frac{1}{2} = -1.6001$

$e^{\frac{1}{2}}$

$3/10/70/0/0/6/75$

$-4.9003 \quad 3/16/39/50$

$7.8006 \quad 77983$

$63.18 = e^{\frac{1}{2}} = 62.84$

$63.18 = e^{\frac{1}{2}} = 62.84$

$63.18 = e^{\frac{1}{2}} = 62.84$

Correct = 50.48483

$e = 4.977$

$e = 4.977$

$e = 4.977$

$e = 4.977$

$e = 4.977$

$e = 4.977$

$e = 4.977$

$e = 4.977$

$e = 4.977$



Feb. 27th  
7th Observation

no 6

45

$$\theta = 22.8 \quad P. 9425 - 1425 = 750$$

$$\text{Vatnat} - 5.46 \quad \begin{array}{r} 850 + 12.9 \\ 830 + 12.9 \\ 817 + 15.0 \\ 800 + 12.8 \\ 825 + 14.5 \\ 848 + 12.8 \\ \hline 5050 + 70.9 = 5120.9 \end{array}$$

$$\text{Vatnat } 6.15 \quad \begin{array}{r} 850 + 12.9 \\ 849 + 12.9 \\ 807 + 15.7 \\ 860 + 12.8 \\ 825 + 14.5 \\ 847 + 12.9 \\ \hline 5038 + 81.7 = 5119.7 \end{array}$$

$$\begin{array}{r} \text{Diffs} \\ 06068 \quad .04719 \quad 4719 \quad 6478 \quad 4597 \\ 1969 \quad 01949 \quad 5517 \quad 1054 \quad 4550 \\ \hline 91.04079 \quad 6.02730 \quad 4137. \quad 448 \quad 4532 \\ .004532 \quad .004550 \quad 4597 \end{array}$$

G	F		
8.328	—	50.266	$\frac{1}{5026} = .01989$
8.554	—	50.252	
8.664	—	50.4—	
8.414	—	16.450	$\frac{1}{1648} = .06068$
8.644	—	15.450	$\frac{1}{1545} = .06473$
8.612	—	21.166	$\frac{1}{21.19} = .04719$
8.460	—	21.220	
8.344	85.6—	170.0—	$\frac{1}{171.9} = .005817$
8.512	87.6—	173.8—	
8.390			
84922			
8.492			

6:15 P.M.

$$\frac{1}{849} = .1178 \times 1021 = v_1 = .12027$$

$$\log = -1.08015$$

$$\frac{1}{2}'' = -1.54008$$

$$f = 9542$$

$$\begin{array}{r} a \\ -16.4270 \\ 3.7043 \\ -1.0802 \\ \hline -13.2165 \\ -3.6691 \\ \hline 311.5474 \\ -4.5158 \\ \hline 18751 \\ 3264 \\ \hline -2.3409 \\ 1.6091 \end{array}$$

$$\begin{array}{r} -6.9746 \\ -4.5158 \\ \hline -2.4638 \\ .02919 = \frac{e}{a} \\ \hline e\gamma_3 \\ 311.5474 \\ -4.8993 \\ \hline -7.7986 \\ 62.88 = e\gamma_3 = 62.82 \end{array}$$

$$\begin{array}{r} 1198 \quad 1178 \quad 1178 \\ 1969 \quad 4719 \quad 5517 \\ \hline 301.13769 \quad 361.16499 \quad 271.1236 \\ 4590 \quad 4583 \quad 4580 \end{array}$$

$$\text{mean of both} = 4572 \times 1021 = v_1 + v_2 = .004668$$

$$\log = -3.669131$$

$$\begin{array}{r} -1.54008 \\ \hline 3.1983 \\ 6.407511 \\ 3.70927 \\ \hline 10.69824 \end{array}$$

$$\begin{array}{r} 4992 \\ 4 \\ \hline e_1 = 4.988 \\ e_1 = 4.982 \\ 1469 \text{ low} \end{array}$$

This is the  
very quietest  
day I have  
seen  
and indeed  
very low  
91%  
his values  
e, b, c, d  
and e b  
.06%

Wednesday - Feb. 28 - 1912

$\theta = 22.8$   $P = 6092 - 39.00 = 1.92$

First Observation,  
5:00 P.M.

Value at 4.55 =  $853 + 12.8 = 865.8$

G		F	
31.0	—	—	—
32.0	—	—	—
31.2	61.6	—	9.9
30.4	63.8	—	10.1
4,46	125.4		
31.15	62.7		

$$\frac{1}{10} = \frac{.1000}{.01595}$$

$$.11595 \times 1021 = .11838 = v_1 + v_2$$

$$\log = -1.0738$$

$$-1.1059$$

$$-3.1983$$

$$-5.3775$$

$$2.9374$$

$$-8.4401$$

$$C_n = 275.5$$

$$e_1 = 138.0 \quad 91.8 \quad 69.0 \quad 55.1$$

$$\log = -2.2117$$

$$\frac{1}{2} n = -1.1059$$

Can't compute

$$\begin{array}{r} a \\ -16.470 \\ 2.9374 \end{array}$$



Second Observation Wed - Feb. 28 -  $\theta = 22.8$   $P = 58.38 - 61.49$   
 $= 3.11$   
 Volts at 5.41 =  $850 + 12.5 = 862.5$

5:25

209

G	F	
10.504	8.108	$\frac{1}{8.093} = .1236$
10.566	8.064	
10.628	8.106	
	15.770	
10.636	15.704	$\frac{1}{15.789} = .06333$
10.578	15.834	
10.836	23.64	
10.588	8.018	$\frac{1}{8.02} = .1247$
10.544	15.826	$\frac{1}{15.8} = .06329$
10.586	15.770	
10.486	28.440	$\frac{1}{28.42} = .03519$
	14.3 - 28.4 -	
10.570	28.418	
	14.2 - 28.4 -	
10.458	30.662 (?)	$\frac{1}{30.66} = .03261$
14.6080		
10.582		

$$\begin{array}{r} .1236 \\ .6333 \\ \hline 24 \overline{) 0.6027} \\ .007511 \end{array} \quad \begin{array}{r} .06329 \\ .3519 \\ \hline 11 \overline{) 0.2870} \\ .002554 \end{array} \quad \begin{array}{r} 1247 \\ .6329 \\ \hline 24 \overline{) 0.6141} \\ .002558 \end{array} \quad \begin{array}{r} 3219 \\ .3261 \\ \hline .00258 \end{array}$$

$$\begin{array}{r} .09452 \\ .1236 \\ \hline 24 \overline{) 2.1812} \\ .002536 \end{array} \quad \begin{array}{r} .09452 \\ .06333 \\ \hline 6 \overline{) 1.5785} \\ .2543 \end{array} \quad \begin{array}{r} 9452 \\ .3519 \\ \hline 5 \overline{) 12.971} \\ .002541 \end{array}$$

$$m = .002541 \times 1021 =$$

$$V_1 + V_2 = .002544$$

$$\begin{array}{r} \log = -3.41404 \\ -1.49227 \\ \hline 3.19836 \\ -6.10407 \\ \hline 2.93557 \\ -4.16870 \\ \hline 9.1685 \\ 14.76 \\ 14.75 \text{ Confirmed} \\ \hline e = 14.75 \end{array}$$

Finished at 5:40  
 $\frac{1}{10.58} = .09452 \times 1021 = V_1 = .096504$

$$\log -2.98454$$

$$\frac{1}{2} i = -1.49227$$

$$l = .002301$$

206

$$\begin{array}{r} 16.4240 \\ -2.9354 \\ \hline 13.4886 \\ -14.3404 \\ \hline -3.4140 \\ 3 \overline{) 12.9269} \\ -4.3090 \\ \hline .4928 \end{array}$$

$$\begin{array}{r} -4.8547 \\ .4928 \\ \hline -4.3619 \\ -4.3094 \\ \hline .0508 \\ .0529 \end{array} \quad \begin{array}{r} 4240 \\ 1130 \\ \hline \end{array}$$

$$.0002046 = a$$

$$\begin{array}{r} 9.1682 \\ 3 \overline{) 18.3364} \\ 6.1121 \\ \hline 12.9955 \\ 3 \overline{) 9.1687} \\ -3.05623 \\ \hline 6.11245 \\ 12.9955 \end{array} \quad \begin{array}{r} 10.46136 \\ 2.93557 \\ \hline 7.39686 \\ -3.41404 \\ \hline 3.98282 \\ -4.3090 \\ \hline -1.67382 \\ .0002 \\ \hline -1.67402 \\ .32598 \\ \hline 2.1185 \\ 2.1185 \end{array}$$

$$\begin{array}{r} 2.1185 \\ 2.1185 \\ \hline 4.2370 \\ -4.2370 \\ \hline 0 \end{array}$$

$$A = .9900$$

Third Observation Wed. Feb. 28.  $\theta = 22.8$

$P = 61.74 - 5809$   
3.65

No 8

Volts at.  $848 + 12.4 = 860.4$   
620

G	F
17.6 — 35.8 —	21.7 —
— 35.584	22.080
— 35.912	22.036
18.0 — 36.2 —	22.196
17.6 — 35.2 —	21.940
— 35.872	22.398
— 35.4 —	29.4 — 57.8 —
18.0 — 35.5 —	29.0 — 57.6 —
17.5 — 35.2 —	29.0 — 57.7 —
18.0 — 35.5 —	19.3 — 37.8 —
17.6 — 35.2 —	19.2 — 38.6 —
— 35.6 —	18.6 — 37.6 —
17.6 — 35.8 —	18.9 — 37.5 —

Differences

$$\begin{array}{r} .04519 \\ + 1733 \\ \hline 3,02786 \\ 00904 \end{array}$$

$$\begin{array}{r} 2641 \\ 1733 \\ \hline 26908 \end{array}$$

$$\begin{array}{r} .02806 \\ + 4519 \\ \hline 8,07328 \\ 0091605 \end{array}$$

$$\begin{array}{r} 2806 \\ 1733 \\ \hline 2641 \\ 405450 \\ 009083 \end{array}$$

$$\frac{1}{22.13} = .04519$$

$$\frac{1}{57.7} = .01733$$

$$37.875 = 26.41$$

$$\text{mean} = 0.9109$$

$$1.021 = 0.9287$$

$$\log = -3.9678$$

$$-1.2287$$

$$3.19726$$

$$-6.39437$$

$$-2.93005$$

$$-9.4599$$

$$e = 2.880$$

$$3.2918$$

$$3.2918$$

$$\begin{array}{r} 3.19956 \\ - 6.3062 \\ \hline e = 2.024 \end{array}$$

$$Q = .0001461$$

$$-4.8547$$

$$5625$$

$$-4.2922$$

$$-5.9485$$

$$34307$$

$$2307$$

$$2307 = \frac{Q}{a}$$

$$\begin{array}{r} 31-9.5106 \\ -3.1707 \\ \hline -6.3404 \end{array}$$

$$\begin{array}{r} ah \\ -10.4616 \\ 2.9350 \\ \hline -7.39636 \\ -3.9678 \\ \hline -5.42856 \\ -5.9485 \\ \hline -1.48006 \\ 0.0025 \end{array}$$

$$219.0 = e^2$$

$$ah = -1.48031$$

$$L_K = .57969$$

$$K = 3.3090$$

$$1-K = 2.3090$$

$$\log = .26324$$

$$-3.4890$$

$$-4.8744$$

$$5.1488$$

$$.36344$$

$$3437$$

$$.1987$$

$$A = 10.46$$

$$a = .09$$

$$76.4220$$

$$-2.4573$$

$$+2.1350$$

$$-15.8132$$

$$-3.9678$$

$$31-13.8454$$

$$-5.9483$$

$$.5625$$

$$-4.51100$$

$$-3.4890$$

$$4.890$$

$$.00069 = a$$

$$3088$$

$$3088$$

$$3088 = \frac{1}{a}$$

$$3155 = \frac{1}{a}$$

$$3155$$

Beauty for low pressure

Corrected Aug 26

No 68

20) Thursday Feb. 29<sup>th</sup> 1912  $\theta = 28.88$   $P = 61.98 - 57.80 = 4.18$   
 First Observation 4:40. Only one bank of battery used  
 $V_{\text{total}} 4:40 = 1850 + 12.9 = 1862.9$   
 $V_{\text{total}} 5:26 = 849 + 12.9 = 861.9$

This drop flickers as though  
 it were unsymmetrical - in shape -

G		F	
8.680	—	12.834	
8.774	—	12.740	
8.824	—	12.902	
8.652	—	40.402	(2) →
8.760	153	50.4—	→
	—	50.338	
8.762	—	51.—	
8.704	—	51.—	
8.766	—	51.6—	
8.788	—	51.4—	
8.804	—	51.632	
8.616	26.6	52.6—	
8.856	—	51.434	
8.724	—	51.128	
8.672	—	51.028	→
8.754	—	43.750	
8.778	—	43.758	→
		71.6—	→
8.764		70.270	→
		78.390	→
		78.0—	
		77.892	→
		56.466	
		56.0—	→

Finished at 5:25



2<sup>nd</sup> Observation - Feb. 27<sup>th</sup> 1912  $\theta =$   $P =$

101  
(19)

$$\begin{aligned} \text{Volts at } 5:26 &= 849 + 12.9 = \underline{861.9} \\ \text{(2 transposed)} & \quad 849 + 12.9 = \underline{861.9} \\ & \quad \quad \quad = 1723.8 \end{aligned}$$

4





Second Observation Mar. 1<sup>st</sup> 1912  $\theta = 23.0$

$$\begin{aligned} \rho &= 62.49 - 57.20 = 5.29 \\ \rho &= 62.48 - 57.20 = 5.28 \\ 827 + 14.4 &= 841.4 \\ 830 + 14.2 &= 844.2 \\ \hline &1685.6 \end{aligned}$$

5:05

Volts at 4:55 P.M.

G	F
9.264	8.862
4.144	8.792
	8.784
9.094	16.244
9.104	16.118
9.094	16.278
9.156	44.298
9.108	44.498
9.144	58.534
9.076	58.482
9.086	40.212
	40.348
	40.328
9.060	33.0 - 1 div.
	31.4 - 2 "
	32.6 - 3 "
	32.6 - 4 "
	31.4 - 5 "
	30.6 - 6 "
	30.0 - 7 "
	30.4 - 8 "
	252.00 -
	31.6 - 1 <sup>st</sup> div.
	31.4 - 2 "
	30.4 - 3 "
	30.6 - 4 "
	30.4 - 5 "
	31.0 - 6 "
	29.2 - 7 "
	29.2 - 8 "

Volts at 5:55 P.M.

$$\frac{1}{8.813} = .1135$$

$$\frac{1}{16.21} = .06169$$

$$\frac{1}{44.40} = .02252$$

$$\frac{1}{58.51} = .01709$$

$$\frac{1}{40.30} = .02481$$

Left readjusted and readings are more reliable hereafter

$$\frac{1}{252} = .003968$$

$$\begin{aligned} 825 + 14.5 &= 839.5 \\ 830 + 14.2 &= 844.1 \\ \hline &1683.6 \end{aligned}$$

Differences

$$\begin{array}{r} .1135 \quad 6169 \quad 2252 \quad 2481 \\ 6169 \quad 2252 \quad 1709 \quad 1709 \\ \hline 201.05141 \quad 1513917 \quad 200543 \quad 320772 \\ \hline .002590 \quad 2606 \quad 271 \quad 257 \end{array}$$

$$\begin{array}{r} 2481 \quad .01709 \quad 2590 \\ 2968 \quad 397 \quad 2606 \\ \hline 81.020842 \quad 510312 \quad 2605 \\ \hline .002605 \quad .002602 \end{array}$$

$$\begin{array}{r} .1099 \quad 1099 \quad 1099 \\ 1135 \quad 6169 \quad 2251 \\ \hline 861.2234 \quad 6617159 \quad 5113241 \\ \hline .002602 \quad .002602 \quad .002609 \end{array}$$

$$\begin{array}{r} .1099 \quad 1099 \quad 1099 \\ 1709 \quad 2481 \quad 2481 \\ \hline 441.12694 \quad 5113471 \quad 119868 \\ \hline .002595 \quad 2593 \quad 2591 \end{array}$$

$$\text{mean} = .02549 \times 1021 = V_1 + V_2 = .02652$$

$$\begin{array}{r} a \\ -16.4289 \\ 3.2264 \\ \hline -1.0503 \\ -14.698676 \\ 3.4235 \\ \hline 31.1127514 \\ -4.4247 \\ \hline -4.4247 \end{array}$$

$$\begin{array}{r} l = .0001354 \\ -4.8547 \\ 7230 \\ \hline -4.1317 \\ -4.4247 \\ \hline 7.7040 \\ 2659 \quad .5093 = a \\ \hline .0002668 = a \end{array}$$

$$\begin{array}{r} \log = -3.4235 \\ \log = -1.5251 \\ \log = -3.1478 \\ -6.1464 \\ 3.2264 \\ \hline -10.4209 \end{array}$$

$$\begin{array}{r} a_k \\ -10.46136 \\ 2.2264 \\ \hline -7.68776 \\ -3.4235 \\ \hline -4.26426 \\ -4.4247 \\ \hline -7.63956 \\ 1.6014 \\ \hline 1.9469 \\ 2.95645 = \end{array}$$

$$\begin{array}{r} 243.80 - \\ 227.40 - \\ \hline 16.40 \end{array}$$

$$\begin{array}{r} 7230 \\ -3.1478 \\ \hline 12.8492 \\ 8523 \end{array}$$

$$e_1 = 8.318$$

$$\begin{array}{r} -16502 \\ -17090 \\ \hline -19432 \\ 1.65820 \\ 1.8523 \\ \hline -1.77990 \\ 6.467 \end{array}$$

$$\log = 1.0503$$

$$\log = -1.52595$$

$$\begin{array}{r} 31.10200 \\ -4.4733 \\ \hline 7.9466 \\ 88.42 = e^{\frac{2}{3}} \end{array}$$

$$\begin{array}{r} 1.65820 \\ 1.8523 \\ \hline -1.77990 \\ 6.467 \end{array}$$

Good one. worked out any 26

11059







106

$$2 + 99 + 40.9 = 2540.4$$

[http://resolver.caltech.edu/CaltechN-I-N\\_Millikan\\_R-1](http://resolver.caltech.edu/CaltechN-I-N_Millikan_R-1)







<sup>12</sup> Third Obs - Mar. 4, 1912

$$\theta = \frac{23.45}{23.42} \left( \frac{\text{begin}}{\text{end}} \right) \quad p = 64,20 - 55.17 = 9.03$$

9.015 at 23

6.05

hwg

Valts at 5:55

$$\begin{array}{r} 828.0 + 14.3 \\ 830.5 + 14.1 \\ \hline 834.0 + 13.5 \\ \hline 2492.5 + 41.9 = 2534.4 \end{array}$$

$$\begin{array}{r} 827.0 + 14.3 \\ 830.0 + 14.1 \\ \hline 833.0 + 13.7 \\ \hline 2490.0 + 42.1 = 2532.1 \end{array}$$

Volbat 6:35

G	F
19.124	
19.220	
19.346	46.760
19.348	47.332
	47.224
	27.348
	27.350
19.116	27.422
	95.564
19.162	47.0 - 1+2 dw
	47.0 - 3+4 dw
	47.0 - 5+6 dw
	46.4 - 7+8 dw
	187.4 —
19.276	
	63.016
<del>19.444</del>	62.846
31.1598	

$$\frac{1}{47.28} = .02115$$
  
$$\frac{1}{27.37} = .03654$$

⑥  $\frac{1}{45.6} = 0.046$

$$\frac{1}{1874} = .005336$$
  
$$\frac{1}{6293} = .01590$$

Good,  
Completed Aug '86  
No 54

$$\begin{array}{r} 02624 \\ 2115 \\ \hline 01539 \\ 5130 \\ \hline 1590 \\ 5336 \\ \hline 210564 \\ \hline 5282 \end{array}$$

$$\begin{array}{r}
 5788 \\
 215 \\
 \hline
 14 \overline{) 7309} \\
 \underline{5246} \\
 2063
 \end{array}
 \qquad
 \begin{array}{r}
 5788 \\
 3654 \\
 \hline
 17 \overline{) 8548} \\
 \underline{5200} \\
 3348
 \end{array}
 \qquad
 \begin{array}{r}
 5788 \\
 1046 \\
 \hline
 12 \overline{) 6240} \\
 \underline{5200} \\
 1040
 \end{array}$$

$$\frac{1}{1.25} = 0.8 \times 100 = 80\%$$

[illegible]

$1 + \sqrt{2} = 0.05205110121 \approx 0.05214$   
 $q = -3.72580$   
 $-1.3640$   
 $3.19776$   
 $6.28714$   
 $2.4036$   
 $10.88356$   
 $11.8873$   
 $7.6614$   
 $8843$   
 $3147686$   
 $7.9224$   
 $83.73 = e^3$   
 $e_1 = 7.6614$   
 $\rightarrow$  related to Cherni come to 83.73

4054

Tuesday, Mar. 5, 1912 -  
at 5:12 P.M.

$\theta = 23.03$

$p = 564.50 - 54.80 = 9.70$

2% Solution Cupric  
Chloride used in first  
Cooling tank (flat tank)

G	F
24.388	34.9 - 12 div
24.612	33.7 - 34 "
24.182	35.4 - 54 "
24.276	35.2 - 74 "
24.254	139.2 -
	43.740
	25.664
	25.770
	25.578
	25.618
	36.6 - 2 div
	37.4 - 4 div
	37.4 - 6 "
	37.6 - 8 "
	148.0
24.274	37.4 - 2 div
	37.0 - 4 div
	37.0 - 6 div
	36.6 - 8 div
	148.0
24.314	

5:40 P.M.

$$\frac{1}{2433} = .04110 \times 1021 =$$

$$V_1 = .041463$$

$$\log = 2.62387$$

$$\frac{1}{2} = 1.31194$$

10.46136  
3.5300  
7.93136  
3.91200  
4.01936  
4.2206  
1.85776 = 6x  
1.4224 = 1/4  
1.3877 = 5  
4.5885  
1.7925  
4.7920

15.885  
1.6471  
9.412

32 000 6251

A = 87.35

just  
mixed  
out Aug 27

Val at 5:00 A.M.  
~~1010~~

834.0 + 13.5 = 847.5  
836.0 + 13.5 = 849.5  
848.5 + 13.7 = 862.2  
829.0 + 14.1 = 843.1  
838.0 + 13.3 = 851.3  
~~852.0 + 13.7 = 865.7~~  
504.6 + 50.1 = 554.7 (4244.6)  
833.0 + 13.6 = 846.6  
834.5 + 13.4 = 847.9  
840.0 + 12.7 = 852.7  
827.0 + 14.3 = 841.3  
3334.5 + 54.9 = 3389.4

Differences

2264 3895 3895  
7144 2268 6757  
2 15656 2 1674 32293  
7828 8056 8048

4110 4110 4110 4110  
7164 1243 3895 6757  
6 48284 6 6398 8005 6 47867  
1006047 007998 8005 7976  
5005 5005 5005 5005

Mean 508945 x 1021 = 7991  
 $V_1 + V_2 = .0081880$   
 $\log = -3.91309$   
 $\frac{1}{2} V_1 = 1.31194$   
-3.19776  
6.42270  
3.5300  
10.89290

$e_1 = 7.8109$  error .5%

$e_2 = 7.745$  in demand for chlorine  
 $e_3 = 7.763$

3 197854 7.9285 3 197854  
7.9285 3 197854  
84.63 7.9285  
84.63 7.9285  
84.63 7.9285

1058

10) March 5, 1912 - 2nd Obs.

$$\theta = \begin{cases} 23.00 \\ 23.05 \end{cases}$$

$$p = 64.69 - 54.59 = 10.10$$

6:05

no 9

Volts at 5:52.

$$\begin{aligned} 833.0 + 13.6 \\ 835.5 + 13.4 \\ 839.0 + 13.8 \\ 827.0 + 14.2 \\ \hline 3334.5 + 54.0 = 3388.5 \end{aligned}$$

Volts at 6:15 P.M.

$$\begin{aligned} 817.0 + 15.0 \\ 824.5 + 14.5 \\ 827.0 + 14.3 \\ 821.0 + 14.8 \\ \hline 3289.5 + 68.6 = 3358.1 \end{aligned}$$

Difference =

$$\begin{aligned} 0.330 \\ 0.222 \\ \hline 0.108 \end{aligned} \quad \text{too small because of dropping voltmeter}$$

$$\begin{array}{r} 0.6675 \\ 0.2222 \\ \hline 8897 \\ 0.1112 \end{array} \quad \begin{array}{r} 6675 \\ 3330 \\ \hline 10005 \\ 0.1112 \times 1021 \end{array}$$

$$= V_1 + V_2 = 0.11353$$

$$0.005677$$

$$\begin{aligned} \log = -2.055123 \\ -1.41673 \\ -3.1463 \end{aligned}$$

$$\log = -3.7541$$

Volts 3370

$$R = 0.00007067$$

$$\begin{aligned} a \\ -16.4270 \\ 3.5286 \\ -2.5333 \\ \hline -14.7886 \\ -3.7541 \\ \hline -18.5427 \\ 3) -18.5427 \\ \hline -4.3447 \\ 1.0043 \\ \hline -3.3404 \\ 2.6510 \end{aligned}$$

$$\begin{aligned} -4.8547 \\ 1.0043 \\ -5.8590 \\ -4.3449 \\ -1.5057 \\ 32.05 = \frac{1}{a} \\ \hline 32.05 \end{aligned}$$

$$\frac{4467}{4468} = \frac{1}{\mu a}$$

$$\begin{aligned} -6.67015 \\ 3.52764 \\ \hline 9.14251 \end{aligned}$$

$$13.885$$

$$\begin{aligned} 2) 13.885 \\ \hline 6.9425 \end{aligned}$$

$$e^{\frac{1}{2}}$$

$$\begin{aligned} 3) -10.8416 \\ -4.9472 \\ \hline -7.8944 \end{aligned}$$

$$78.42 = e^{\frac{1}{2}}$$

Error .69 am  
acc of voltmeter

$$e^{\frac{1}{2}} = 78.42$$



Mar. 6<sup>th</sup> 1912

First Observation  
4:52

$$\theta = \frac{23.00 \text{ begin}}{23.13 \text{ end}} \quad \rho = \frac{6473 \text{ (in)}}{4861} \quad \frac{6474 \text{ (milli)}}{4861} \times 9$$

Valto at 4:45

$$\begin{aligned} 832.5 + 13.8 \\ 834.0 + 13.7 \\ 838.0 + 13.3 \\ 824.0 + 14.5 \\ 833.0 + 13.8 \\ 834.5 + 13.7 \\ \hline 4996.0 + 82.8 = 5078.8 \end{aligned}$$

No 10

41

Valto at 5:55

$$\begin{aligned} 830.0 + 14.1 \\ 832.0 + 13.9 \\ 836.0 + 13.5 \\ 821.5 + 14.7 \\ 832.5 + 13.8 \\ 832.0 + 13.9 \\ \hline 4983.0 + 84.0 = 5067.0 \end{aligned}$$

Beauty

G	F
14.302	
14.288	
14.218	(42.2)
14.228	
14.298	
14.218	
46.6 - 12 <sup>th</sup> division	
47.8 - 2 <sup>nd</sup> "	
47.2 - 3 <sup>rd</sup> "	
47.0 - 4 <sup>th</sup> "	
48.0 - 5 <sup>th</sup> "	
47.4 - 6 <sup>th</sup> "	
48.0 - 7 <sup>th</sup> "	
48.0 - 8 <sup>th</sup> "	

Included only  
below line  
beginning of change in G.

$$\begin{aligned} 14.228 \\ \times 2.2 \\ \hline 31.8 \\ 50.0 \end{aligned}$$

14.204

13.966

14.072

14.082

14.118

14.092

14.184

14.018

13.944

13.476

14.06

14.061

14.061

14.061

14.061

14.061

14.061

$$\begin{aligned} 112.0 - \frac{1}{112} &= 0.08929 \\ 26.258 - \frac{1}{26.25} &= 0.3540 \\ 23.758 - \frac{1}{23.75} &= 0.4214 \\ 65.296 - \frac{1}{65.30} &= 0.01531 \\ 45.616 - \frac{1}{45.62} &= 0.2182 \\ 35.122 (35.4) - \frac{1}{35.28} &= 0.2835 \\ 35.434 (35.4) - \frac{1}{35.28} &= 0.2835 \\ 119.0 - \frac{1}{119.2} &= 0.00389 \\ 119.4 - \frac{1}{119.2} &= 0.00389 \end{aligned}$$

5:53 P.M.

$$\begin{aligned} -16.127009 & -4.4547 \\ 3.705050 & 1.3249 \\ -3.267101 & -5.5300 \\ -14993160 & -4.3871 \\ -3.831000 & -1.1429 \\ 3/11.161250 & 1394 \\ -4.3871 & 3453 \\ 1.3247 & 2129 \\ -3.7118710 & 1450 \\ 2.2862 & 1944 \\ \hline & 1944 \end{aligned}$$

Differences

$$\begin{aligned} 3540 & 14214 & 04214 & 2835 & 2164 \\ 6929 & 03540 & 01581 & 8369 & 1361 \\ 1026471 & 00674 & 102643 & 119961 & 601 \\ 006618 & & 006708 & 665 & \\ & 4214 & 6706 & & \\ & 8929 & 6616 & & \\ & 5/33211 & 6650 & & \\ & 6642 & 6640 & & \\ & & 4126616 & & \\ & & 006654 & & \text{mean of diff} \end{aligned}$$

$$\begin{aligned} .07449 & .07049 & 7049 & 7049 \\ 6929 & 4214 & 2835 & 2164 \\ 12/07449 & 17/07049 & 15/7049 & 14/7049 \\ .006658 & .006654 & .006628 & .006623 \\ 6672 & 6663 & 6623 & 6633 \\ \text{Mean} = .006650 \times 4.021 = & & & \\ v_1 + v_2 = .006762 & & & \\ \log = -3.8300 & & & \\ -1.4300 & & & \\ 3.1963 & & & \\ -6.4588 & & & \\ 3.7050 & & & \\ 10.7538 & & & \\ \text{Value} = 5070 & & & \\ e = 5.644 & & & \\ e^3 = & & & \\ 31-10.7558 & & & \\ -4.4888 & & & \\ -7.8392 & & & \\ 4246770 & & & \end{aligned}$$

$$\begin{aligned} \log = -2.8601 \\ \frac{1}{2} = -1.4300 \end{aligned}$$

4) Thursday - Mar. 7<sup>th</sup> 1912

$\theta = 23.70^\circ$   $p = \frac{6993}{4840} = 1.445$   
Volts at 3:15  $\frac{1}{5}$  min  $\frac{21.53}{1}$

Volts at 3:15

3:35 P.M.

G	F	
<del>16.322</del>	(28.6) (57.2-)	$\frac{1}{57.2} = 0.01748$
16.190	153.0 307.4-	$\frac{1}{307.4} = 0.003253$
16.184	174.0 349.0-	$\frac{1}{349} = 0.002865$
16.184	51.0 102.0-	$\frac{1}{102} = 0.009804$
16.184	207.6 413.8-	$\frac{1}{413.8} = 0.002415$
15.996	— (42.0-)	$\frac{1}{42.01} = 0.02381$
	— 47.006	
	— 60.314	$\frac{1}{60.31} = 0.01658$
	(60.6-)	

$$\begin{array}{r} 30646 \\ 1613 \end{array}$$

$$\frac{1}{1.13} = .8850 \times 1.21 = V_1 = .06228$$

$$L_{04} = -2.7144$$

$$\frac{1}{2}v_1 = -1/3472$$

$$\begin{array}{r} 76.4270 \\ 3.7067 \\ -2.7844 \\ \hline 14.9281 \\ -3.8652 \\ \hline 3/11.0629 \\ -4.3543 \\ \hline 1.2330 \\ -3.6873 \\ \hline 2.3122 \end{array}$$

600 2161 20

$$205.4 = \frac{1}{f_m}$$

$$\begin{array}{r} -4,8549 \\ 13370 \\ \hline -5,5217 \\ -43543 \\ \hline =-61674 \end{array} \quad .147$$

$$\begin{array}{r} 841.5 + 13.2 \\ 841.5 + 13.2 \\ 845.0 + 13.0 \\ 814.0 + 15.3 \\ 843.5 + 13.1 \\ 843.0 + 13.1 \\ \hline 5028.5 + 80.9 = 5109.4 \end{array}$$

*diffusum*

$$\begin{array}{r} 0.2381 \\ 0.02415 \\ \hline 3 \overline{) 0.23815} \\ 0.07132 \\ \hline 0.09504 \\ 0.02885 \\ \hline 0.06619 \\ 0.07164 \end{array}$$

06200	06200	6200	6200	6200
002865	9804	2415	2381	1658
9/ 064865	10 071504	9 6441	12 8631	11 7855
007207	007180	007157	2191	716

$$\text{mean} = .007179 \times 1021$$

$$= k_1 + k_2 = 0073317$$

$$\begin{array}{r} \log = -3.8652 \\ -1.3472 \\ 3.1983 \\ \hline -6.4607 \end{array}$$

$$\text{mean wlls} = 5790 \quad \frac{3.7067}{10.7540}$$

$$e_1 = \underline{5694} \quad | \quad 19,51006$$

- 7.8367

$$e^2 = 6870$$

Y  
This is the first one  
a little irregular  
The one is good  
It comes about  
before line  
replaced

Second Observation  
Mar. 7<sup>th</sup> 1912

$$\theta = \frac{23.48}{23.54}$$

$$p = \frac{7011}{4220} = 1.661$$

(7)

Volts at 4115

$$834.5 + 13.7$$

$$837.0 + 13.4$$

$$839.5 + 13.2$$

$$811.5 + 15.5$$

$$839.0 + 13.2$$

$$839.0 + 13.2$$

$$5000.5 + 82.2 = 5082.7$$

G	F
9.132	
9.086	42.138
	(21.2) (21.4-)
	53.554
	(27.0) (54.0-)
90.76	53.300
	(27.0) (53.6-)
9.232	53.420
	(27.6) (53.8-)
9.124	



6) Third Observation  
March 7, 1912.  
5:55

$$\theta = \frac{23.41}{23.63}$$

$$p = \frac{70.50}{47.77}$$

Velts at 5:48

G		F
16.704	16.704	16.704
24.312		20.728
24.326		20.540
24.256		20.728
24.128		

6:10 P.M.

$$\begin{aligned} &830.0 + 14.1 \\ &833.0 + 13.8 \\ &836.0 + 13.5 \\ &807.0 + 15.7 \\ &833.0 + 13.8 \\ &833.0 + 13.8 \\ &4972.0 + 84.7 = 5056.7 \end{aligned}$$

Fourth Obs. 3/7/12  $\theta = \frac{28.53}{23.53}$ 

$$p = \frac{7073}{4745} = 23.25$$

(5)

6:13 P.M.

Natts at 6:40

B	F
17.094	
17.234	20.872
16.996	19.734
17.064	19.566
17.220	19.562
17.314	54.066
17.134	54.288
17.172	54.280
17.144	27.496
17.094	27.506
	27.658
	46.488
17.118	72.0 142.0-
	73.0 144.5-

6:38 P.M.

$$829.0 + 14.2$$

$$831.0 + 14.0$$

$$833.0 + 13.8$$

$$800.0 + 16.0$$

$$832.0 + 13.9$$

$$832.0 + 13.9$$

$$4957.0 + 85.8 = 5042.8$$

Monday, Nov 11<sup>th</sup> 1912

$$\theta = 23.07$$

$$\phi = 71.00 - 47.14 = 23.86$$

3:35

No 11

3 PM

G	F	F
18.074	24.3	48.3 — $\frac{1}{48.2} = .02075$
18.098	24.0	48.2 — $\frac{1}{71.6} = .01397$
18.276	—	71.6 — $\frac{1}{48.2} = .02068$
18.312	24.0	48.2 — $\frac{1}{48.2} = .02068$
18.230	—	48.5 — $\frac{1}{73.6} = .01359$
18.216	37.0	73.6 — $\frac{1}{49.9} = .02024$
18.352	36.6	73.6 — $\frac{1}{73.8} = .01348$
18.238	25.0	49.4 — $\frac{1}{74.3} = .01345$
18.218	37.0	73.8 — $\frac{1}{74.4} = .01344$
18.212	37.2	74.3 — $\frac{1}{74.4} = .01344$
18.292	37.6	74.4 — $\frac{1}{74.4} = .01344$
18.237	—	29.4 — $\frac{1}{29.4} = .03401$
18.206	—	—
13/29 71°	—	—
18.229	—	—

disregard all this  
in table because value  
must have dropped  
appreciably in this period

Differences

0.2075	2068	.02024	2024
0.1397	1397	.01359	1348
00678	671	.00665	676

03401	676
01348	671
3) 02053	685
006843	676

This difference must  
be added to  
around 1/100

0.06486	5486	5486	5486
0.02075	1359	1348	3401
1) 07561	10) 6845	10) 6634	3) 8887
006874	006845	006634	006836

$$\text{most probable value} = 006838 \times 10^2$$

$$= V_1 + V_2 = 0069815$$

$$\begin{aligned} \log &= -3.8440 \\ &= -1.3742 \\ &= -3.1483 \end{aligned}$$

mean value = 4582

$$\begin{aligned} &= -6.4865 \\ &+ 3.6611 \\ &= -10.7554 \end{aligned}$$

$$\begin{aligned} e_1 &= 5694 \times 10^{-10} \\ e_2 &= 5.687 \end{aligned}$$

error 3%

$e^2$

$$\begin{aligned} 3) 107554 \\ &= 4.9185 \\ &= 7.8370 \end{aligned}$$

$$\begin{aligned} 68.70 &= e^2 \\ &= 6.64 \end{aligned}$$

$$\frac{1}{18.2} = .05486 \times 10^2 = V_1 = .05601$$

$$\log = 2.7483$$

$$\frac{1}{2} = 7.3742$$

$$l = 00002949$$

$$\begin{aligned} &= 4.8547 \\ &= 1.3777 \\ &= 5.4770 \\ &= 4.3308 \\ &= 1.1462 \end{aligned}$$

$$\begin{aligned} 1400 &= l \\ 1405 &= a \end{aligned}$$

a

$$\begin{aligned} &= 164270 \\ &= 3.6611 \\ &= 2.7483 \\ &= 14.8364 \\ &= 3.8440 \end{aligned}$$

$$\begin{aligned} 2) 10.9924 \\ &= 4.3308 \\ &= 1.3777 \\ &= 3.7085 \\ &= 2.2915 \end{aligned}$$

$$.0002142 = a$$

$$1957 = \mu a$$

$$1963$$



Second Obs. Mar. 11, 1912  
(Monday)  
5:28 P.M.

$$\theta = 23.20$$

$$p = \frac{7123}{14690} = 24.33$$

Volt at 4:17

$$\begin{aligned} 659.5 + 15.6 \\ 835.0 + 13.6 \\ 837.5 + 13.5 \\ 503.0 + 04.0 \\ 835.0 + 13.6 \\ 835.0 + 13.6 \end{aligned}$$

$$4505.0 + 73.9 = 4578.9$$

G	F
7.874	<del>23.6</del>
7.862	23.6
7.876	23.9
7.878	23.5
7.792	
7.874	23.734
	23.522
7.902	40.2 79.6
7.918	40.2 79.6
7.852	79.4
7.923	

No 12

39

Volt at 5:15

$$\begin{aligned} 659.0 + 15.0 \\ 834.0 + 13.8 \\ 836.5 + 13.5 \\ 503.0 + 04.0 \\ 834.0 + 13.8 \\ 834.0 + 13.8 \end{aligned}$$

$$4500.5 + 73.9 = 4574.4$$

Difference

$$\begin{array}{r} 0.4252 \\ 0.1268 \\ 7 \overline{) 0.2974} \\ 004244 \end{array}$$

$$\begin{array}{r} 4210 \\ 1268 \\ 2942 \end{array}$$

$$\frac{1}{7875} = 1.270 \times 10^{-2} = 1.2967$$

5:42 P.M.

$$\log = -1.1134$$

$$\frac{1}{2} = -1.55670$$

a

l

$$\begin{aligned} -16.4209 \\ 3.6601 \\ -1.1134 \\ -13.1944 \\ -3.6366 \end{aligned}$$

$$3 \overline{) 11.5583}$$

$$-4.5294$$

$$1.3858$$

$$-3.9052$$

$$2.0948$$

$$\begin{aligned} -4.8547 \\ 1.3858 \\ -5.4684 \\ -4.5194 \\ -2.9490 \end{aligned}$$

$$0.8853 = \frac{1}{2}$$

$$3333 = a$$

$$3309$$

$$1237 = \frac{1}{f_m}$$

$$\begin{array}{r} 1.270 \\ 4232 \\ 40 \overline{) 1.6942} \\ 004230 \end{array}$$

$$\begin{array}{r} 1.270 \\ 1258 \\ 33 \overline{) 13978} \\ 4233 \end{array}$$

$$\begin{aligned} \text{mean} &= 4235 \times 10^{-2} \\ &= v_1 + v_2 = 0.04324 \end{aligned}$$

$$\begin{aligned} \log v_1 + v_2 &= -3.63548 \\ &= -1.55641 \\ &= 3.1943 \\ &= -6.39019 \\ &= 3.6601 \\ &= -10.7301 \end{aligned}$$

$$\begin{aligned} 6361 \\ 5567 \\ 1477 \\ 2905 \\ 6401 \\ 7204 \\ V = 45.72 \end{aligned}$$

$$e = 5375$$

$$e_1 = 5379$$

$$e = 5354$$

$$e = 5379$$

$$e = 5379$$

$$e = 5379$$

$$e = 5379$$

$$\begin{aligned} e\% &= 72.99 \\ &= -10.73046 \\ &= 2 \overline{) -14.4609} \\ &= -7.8203 \end{aligned}$$

$$e_1 = 66.115$$

$$e_2 = 66.115$$

$$e_3 = 66.115$$

$$e_4 = 66.115$$

Monday, Mar. 11, 1912  
Thud Obs.

$$\theta = 23.18 \quad p = \frac{71.70}{46.33} = 23.37$$

Volts at 545

$$\begin{aligned} 659.0 + 15.7 \\ 833.0 + 13.9 \\ 836.5 + 13.5 \\ 502.5 + 03.8 \\ 833.0 + 13.9 \\ 833.0 + 13.9 \\ \hline 4497.0 + 74.7 = 4571.7 \end{aligned}$$

Differences

$$\begin{array}{r} .02785 \\ .01870 \\ \hline .00915 \\ 2 \overline{) .00915} \\ \underline{.004575} \end{array} \quad \begin{array}{r} 4 \overline{) .01870} \\ \underline{.004675} \end{array} \quad \begin{array}{r} 4 \overline{) .01870} \\ \underline{.004675} \end{array}$$

$$\begin{array}{r} 1063 \\ 2785 \\ \hline 13415 \\ 29 \overline{) 13415} \\ \underline{004638} \end{array} \quad \begin{array}{r} 1063 \\ 1870 \\ \hline 12500 \\ 27 \overline{) 12500} \\ \underline{004629} \end{array} \quad \begin{array}{r} 1063 \\ 000 \\ \hline 1063 \\ 25 \overline{) 1063} \\ \underline{004622} \end{array}$$

$$\begin{aligned} \text{mean} &= .004633 \times 1021 \\ &= V_1 + V_2 = .0047303 \end{aligned}$$

$$\begin{aligned} \log &= -3.6749 \\ &= -1.5177 \\ &= -3.1983 \\ &= -8.3909 \\ &= 8.6599 \\ \hline &= -10.7310 \end{aligned}$$

$$\begin{aligned} e_1 &= 5.387 \\ e_2 &= 5.351 \end{aligned}$$

$$\begin{aligned} C_1 &= 66.21 \\ C_2 &= 66.16 \end{aligned}$$

just enough  
error 7%

G	F	
9.440	35.920	
9.458	(18.4) 36.003	$\frac{1}{35.91} = .02785$
9.360	(17.6) 35.818	
9.398	(27.0) 53.472	$\frac{1}{53.47} = .01870$
9.374	(32.4) 53.472	
5 2040	Balanced	
9.408	Speed	
	(very nearly)	

$$\begin{aligned} \frac{1}{9.41} &= .1063 \times 1021 = .1085 = V_1 \\ \log &= -7.0354 \\ \frac{1}{2} &= .7517 \end{aligned}$$

6:10 P.M.

$$\begin{array}{r} a \\ -16.4270 \\ 3.6599 \\ -2.0354 \\ \hline -13.1223 \\ -3.6749 \\ \hline 11.4474 \\ -4.4825 \\ \hline 1.4043 \\ -3.8868 \\ \hline 2.1132 \end{array} \quad \begin{array}{r} l \\ -4.8547 \\ 1.4043 \\ \hline -5.4504 \\ -2.4825 \\ \hline -2.9679 \\ .0925 = l \\ 9330 = a \\ \hline 30375 = 20 \\ 1024 \\ \hline 3022 \\ 1298 = \frac{1}{7a} \\ 1264 \end{array}$$

Period 5  
compare with  
compare diff 44







## Calibration of Hipp Chronograph Lassalle

40 sec interval

$\begin{array}{r} 220.13 \\ 20.21 \\ \hline 4 \overline{) 199.92} \\ 49.98 \end{array}$	$\begin{array}{r} 220.50 \\ 20.13 \\ \hline 4 \overline{) 200.37} \\ 50.09 \end{array}$	$\begin{array}{r} 220.55 \\ 20.50 \\ \hline 4 \overline{) 200.05} \\ 50.01 \end{array}$	$\begin{array}{r} 220.20 \\ 20.55 \\ \hline 4 \overline{) 199.65} \\ 49.91 \end{array}$	$\begin{array}{r} 220.27 \\ 20.20 \\ \hline 4 \overline{) 200.07} \\ 50.02 \end{array}$	$\begin{array}{r} 220.27 \\ 20.27 \\ \hline 4 \overline{) 200.00} \\ 50.00 \end{array}$
$\begin{array}{r} 219.92 \\ 20.27 \\ \hline 4 \overline{) 199.63} \\ 49.91 \end{array}$	$\begin{array}{r} 219.53 \\ 19.92 \\ \hline 4 \overline{) 199.61} \\ 49.90 \end{array}$	$\begin{array}{r} 219.50 \\ 19.58 \\ \hline 4 \overline{) 199.92} \\ 49.98 \end{array}$	$\begin{array}{r} 219.60 \\ 19.50 \\ \hline 4 \overline{) 200.10} \\ 50.02 \end{array}$	$\begin{array}{r} \text{mean} \\ \hline 49.981 \end{array}$	

10 sec interval

$\begin{array}{r} 69.98 \\ 20.60 \\ \hline 49.38 \end{array}$	$\begin{array}{r} 119.14 \\ 69.98 \\ \hline 49.26 \end{array}$	$\begin{array}{r} 70.71 \\ 19.14 \\ \hline 50.55 \end{array}$	$\begin{array}{r} 54.55 \\ 4.46 \\ \hline 50.09 \end{array}$	$\begin{array}{r} 105.31 \\ 54.35 \\ \hline 50.46 \end{array}$	$\begin{array}{r} 55.39 \\ 5.01 \\ \hline 50.38 \end{array}$
$\begin{array}{r} 104.93 \\ 55.39 \\ \hline 49.54 \end{array}$	$\begin{array}{r} 58.82 \\ 8.44 \\ \hline 50.38 \end{array}$	$\begin{array}{r} 109.40 \\ 58.82 \\ \hline 50.58 \end{array}$	$\begin{array}{r} 59.33 \\ 9.40 \\ \hline 49.93 \end{array}$	$\begin{array}{r} 109.91 \\ 9.40 \\ \hline 50.51 \end{array}$	$\begin{array}{r} 60.03 \\ 9.91 \\ \hline 50.12 \end{array}$
$\begin{array}{r} 60.25 \\ 10.27 \\ \hline 49.98 \end{array}$	$\begin{array}{r} 110.58 \\ 60.25 \\ \hline 50.33 \end{array}$	$\begin{array}{r} 60.51 \\ 10.58 \\ \hline 50.23 \end{array}$	$\begin{array}{r} 111.03 \\ 60.81 \\ \hline 50.22 \end{array}$	$\begin{array}{r} 61.33 \\ 11.03 \\ \hline 50.30 \end{array}$	$\begin{array}{r} 111.24 \\ 61.33 \\ \hline 50.21 \end{array}$
$\begin{array}{r} 111.69 \\ 61.49 \\ \hline 50.20 \end{array}$	mean of 15 = 50.12				

4 sec interval

$\begin{array}{r} 31.80 \\ 11.64 \\ \hline 20.11 \end{array}$	$\begin{array}{r} 57.62 \\ 31.80 \\ \hline 20.22 \end{array}$	$\begin{array}{r} 72.11 \\ 51.82 \\ \hline 20.29 \end{array}$	$\begin{array}{r} 92.11 \\ 72.11 \\ \hline 20.20 \end{array}$	$\begin{array}{r} 112.28 \\ 92.11 \\ \hline 20.17 \end{array}$	$\begin{array}{r} 32.77 \\ 12.28 \\ \hline 20.49 \end{array}$	$\begin{array}{r} 52.80 \\ 32.77 \\ \hline 20.03 \end{array}$	$\begin{array}{r} 73.87 \\ 52.80 \\ \hline 20.27 \end{array}$	$\begin{array}{r} 93.05 \\ 73.87 \\ \hline 19.98 \end{array}$
$\begin{array}{r} 113.25 \\ 13.05 \\ \hline 20.20 \end{array}$	$\begin{array}{r} 33.50 \\ 13.25 \\ \hline 20.25 \end{array}$	$\begin{array}{r} 53.94 \\ 33.50 \\ \hline 20.44 \end{array}$	$\begin{array}{r} 74.30 \\ 53.94 \\ \hline 20.40 \end{array}$	$\begin{array}{r} 94.52 \\ 74.30 \\ \hline 20.22 \end{array}$	$\begin{array}{r} 114.77 \\ 94.52 \\ \hline 20.25 \end{array}$	$\begin{array}{r} 34.94 \\ 14.77 \\ \hline 20.22 \end{array}$	$\begin{array}{r} 55.14 \\ 34.94 \\ \hline 20.20 \end{array}$	$\begin{array}{r} 75.40 \\ 55.14 \\ \hline 20.21 \end{array}$
$\text{mean} = 20.21$								

## Key No. 1 for 10 secs

$$\begin{array}{r} 114.04 \\ 63.71 \\ \hline 50.33 \end{array}$$

$$\begin{array}{r} 63.94 \\ 14.04 \\ \hline 49.90 \end{array}$$

$$\begin{array}{r} 113.75 \\ 63.94 \\ \hline 49.81 \end{array}$$

$$\begin{array}{r} 63.88 \\ 13.75 \\ \hline 50.13 \end{array}$$

$$\begin{array}{r} 97.86 \\ 47.65 \\ \hline 50.21 \end{array}$$

$$\begin{array}{r} 148.12 \\ 97.86 \\ \hline 50.26 \end{array}$$

$$\begin{array}{r} 98.09 \\ 48.12 \\ \hline 49.97 \end{array}$$

$$\begin{array}{r} 144.87 \\ 94.66 \\ \hline 50.21 \end{array}$$

$$\begin{array}{r} 94.75 \\ 44.87 \\ \hline 49.88 \end{array}$$

$$\begin{array}{r} 144.86 \\ 94.75 \\ \hline 50.11 \end{array}$$

$$\begin{array}{r} 94.94 \\ 44.86 \\ \hline 50.08 \end{array}$$

$$\begin{array}{r} 144.88 \\ 94.94 \\ \hline 49.94 \end{array}$$

$$\begin{array}{r} 56.49 \\ 6.01 \\ \hline 50.48 \end{array}$$

$$\begin{array}{r} 106.63 \\ 56.49 \\ \hline 50.14 \end{array}$$

Mean of 14 readings  
for 10 sec = 50.104

## Key No. 1 for 4 secs

$$\begin{array}{r} 26.98 \\ 6.63 \\ \hline 20.35 \end{array}$$

$$\begin{array}{r} 47.58 \\ 26.98 \\ \hline 20.60 \end{array}$$

$$\begin{array}{r} 67.78 \\ 47.58 \\ \hline 20.20 \end{array}$$

$$\begin{array}{r} 87.94 \\ 67.78 \\ \hline 20.16 \end{array}$$

$$\begin{array}{r} 108.32 \\ 87.94 \\ \hline 20.38 \end{array}$$

$$\begin{array}{r} 28.83 \\ 8.32 \\ \hline 20.51 \end{array}$$

$$\begin{array}{r} 58.81 \\ 28.83 \\ \hline 29.98 \\ 2 \end{array}$$

$$\begin{array}{r} 79.02 \\ 58.81 \\ \hline 20.21 \end{array}$$

$$\begin{array}{r} 99.48 \\ 79.02 \\ \hline 20.46 \end{array}$$

$$\begin{array}{r} 20.21 \\ 99.48 \\ \hline 20.73 \end{array}$$

$$\begin{array}{r} 3 \overline{) 59.96} \\ 19.99 \end{array}$$

ten readings  
Mean = 20.357 for 4 secs.



# Calibration of Hipp Chronoscope.

Wednes.  
Dec. 6, 1911

*Millikan*

Key No. 1

$$\begin{array}{r} 136.15 \\ 86.09 \\ \hline 50.06 \end{array}$$

$$\begin{array}{r} 96.09 \quad 146.15 \\ 46.15 \quad 96.09 \\ \hline 59.94 \rightarrow \text{for } 50.06 \\ 12 \text{ sec.} \end{array}$$

$$\begin{array}{r} 96.36 \\ 46.15 \\ \hline 50.21 \end{array}$$

$$\begin{array}{r} 146.46 \\ 96.36 \\ \hline 50.10 \end{array}$$

$\therefore 49.95$  for 10 secs.

New Key Key No. 2

$$\begin{array}{r} 96.56 \\ 46.46 \\ \hline 50.10 \end{array}$$

$$\begin{array}{r} 246.51 \\ 96.56 \\ \hline 149.95 \\ 49.98 \end{array}$$

$$\begin{array}{r} 96.25 \\ 46.51 \\ \hline 49.74 \end{array}$$

$$\begin{array}{r} 145.88 \\ 96.25 \\ \hline 49.63 \end{array}$$

$$\begin{array}{r} 245.94 \\ 45.88 \\ \hline 200.06 \\ 50.00 \end{array}$$

$$\begin{array}{r} 258.65 \\ 58.93 \\ \hline 4 | 199.72 \\ 49.93 \end{array}$$

$$\begin{array}{r} 245.96 \\ 45.94 \\ \hline 4 | 200.02 \\ 50.00 \end{array}$$

$$\begin{array}{r} 245.70 \\ 45.96 \\ \hline 4 | 199.740 \\ 49.94 \end{array}$$

$$\begin{array}{r} 258.59 \\ 58.65 \\ \hline 4 | 199.94 \\ 49.99 \end{array}$$

$$\begin{array}{r} 258.31 \\ 58.65 \\ \hline 4 | 199.66 \\ 49.92 \end{array}$$

$$\begin{array}{r} 257.66 \\ 58.31 \\ \hline 4 | 199.35 \\ 49.84 \end{array}$$

Key No. 1

$$\begin{array}{r} 257.59 \\ 257.66 \\ \hline 4 | 199.93 \\ 49.98 \end{array}$$

$$\begin{array}{r} 264.74 \\ 64.95 \\ \hline 4 | 199.79 \\ 49.95 \end{array}$$

$$\begin{array}{r} 264.69 \\ 64.74 \\ \hline 4 | 199.95 \\ 49.99 \end{array}$$

$$\begin{array}{r} 264.73 \\ 64.69 \\ \hline 4 | 200.04 \\ 50.01 \end{array}$$

$$\begin{array}{r} 264.63 \\ 64.73 \\ \hline 4 | 199.90 \\ 49.98 \end{array}$$

$$\begin{array}{r} 264.55 \\ 64.63 \\ \hline 4 | 199.92 \\ 49.98 \end{array}$$

$$\begin{array}{r} 264.83 \\ 64.55 \\ \hline 4 | 200.28 \\ 50.07 \end{array}$$

$$\begin{array}{r} 264.71 \\ 64.93 \\ \hline 4 | 199.88 \\ 49.97 \end{array}$$

Mean of 10 obs. on 40 secs. at  $18^{\circ}\text{C}$   
 $\div 4 = 49.975 = 10 \text{ secs}$

Feb 10<sup>th</sup> 1912  
Calibration of Hipp's chronoscope for 5 sec interval

1st len readings	54.65	29.75	29.30	54.06	79.16	103.67
	<u>29.75</u>	<u>4.73</u>	<u>4.30</u>	<u>29.30</u>	<u>54.06</u>	<u>79.16</u>
	24.90	25.02	24.80	24.76	25.10	24.71

28.90	54.19	79.23	104.32
<u>3.87</u>	<u>28.90</u>	<u>54.19</u>	<u>79.23</u>
25.03	25.29	25.04	25.09

49.80
5.004
4.96
49.52
5.020
49.42
5.006
50.58
5.008
5.014
49.948
4.995

2nd len readings	24.10	54.22	104.65	
	<u>4.32</u>	<u>29.10</u>	<u>79.42</u>	
	24.78	25.12	25.23	29.63
				<u>4.65</u>
				24.98

54.58	74.86	104.72	30.03	55.21	80.03
<u>29.63</u>	<u>54.58</u>	<u>74.86</u>	<u>74.72</u>	<u>30.03</u>	<u>55.21</u>
24.95	25.28	24.86	25.31	25.18	24.82

4.956
5.024
50.46
49.96
49.90
50.56
49.72
50.62
50.36
49.64
50.102
49.948
2100.050
5.0025

This shows that I can rely on Hipp's chronoscope  
things down to 5 sec with no error larger than  
.2% - might call it .4% for safety then  
I would be in error only .6% at outside,



