



Robert Millikan (top center) on the steps of Ryerson Laboratory, U. of Chicago, 1908. Other colleagues (L-R): A. A. Michelson, Carl Kinsey, Henry G. Gale

ROBERT A. MILLIKAN

Oil Drop Experiment Notebooks

NOTEBOOK ONE:
October 1911-March 1912

PART 1 OF 3
From page 1 to page 39

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Abstract

Robert A. Millikan (1868-1953) began his experiments to measure the charge on the electron, e , in 1907. The experiments were performed in Ryerson Laboratory at the University of Chicago, where Millikan was professor of physics. For this work, and for work on the photoelectric effect, Millikan was awarded the Nobel Prize in physics in 1923.

Millikan gives his own account of the electron charge determination in his published autobiography in the chapter titled "My Oil-Drop Venture (e)" (Robert A. Millikan, *The Autobiography of Robert A. Millikan*, New York, 1950). With the aid of graduate students Louis Begeman, Harvey Fletcher, and J. Y. Lee, Millikan devised the method of measuring the rate of fall of a single electrically charged oil drop under the forces of gravity and electricity. From 1909 until the spring of 1912, Millikan reports, he spent every available moment in the laboratory on his oil-drop experiment. His first comprehensive, though to some extent preliminary, results were published in September 1910 in the journal *Science* as "The Isolation of an Ion, a Precision Measurement of Its Charge, and the Correction of Stokes' Law," *Science* 32: 436-448. He soon became embroiled in a controversy with the Viennese physicist Felix Ehrenhaft, who claimed to have found much smaller electric charges. Millikan went back to work on a new

set of experiments. By the spring of 1912 he had collected the data for what he termed “the final, absolute determination of the numerical value of the electron” (*Autobiography*, p. 84). Results were published in August 1913 in “On the Elementary Electrical Charge and the Avogadro Constant,” *Physical Review* 2: 109-43. This last, definitive set of experiments were recorded in the only two lab notebooks which Millikan preserved among his papers. These two notebooks are presented here in facsimile. They cover the period from October 1911 through April 1912 and contain what Millikan himself considered his conclusive, historic work on this problem.

For an analysis of Millikan’s notebooks and a defense of his experimental method, see the article by David Goodstein, “In Defense of Robert Andrews Millikan,” published in *American Scientist* 89/1 (Jan-Feb. 2001): 54.
<http://www.americanscientist.org/issues/num2/2001/1/in-defense-of-robert-andrews-millikan/1>

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Preferred citation

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California Institute of Technology Archives. Retrieved [supply date of retrieval]
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http://resolver.caltech.edu/CaltechLN:LN_Millikan_R_1

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Thermometer Readings and Corrections-

Standard	Bickman	$\frac{1}{10}^{\circ}$ small stem (.15° low)	$\frac{1}{10}^{\circ}$ large stem
22.79	1.76		
22.81	1.78		
23.00	1.97	22.85	22.95 (?)

Corrections to Standard Thermometer.

	0	.1	.2	.3	.4	.5	.6	.7	.8	.9
22°	-0.025	-0.025	-0.025	-0.025	-0.024	-0.024	-0.024	-0.023	-0.023	-0.023
23°	-0.023	-0.022	-0.022	-0.022	-0.022	-0.022	-0.021	-0.021	-0.021	-0.021
24°	-0.021	-0.020	-0.020	-0.020	-0.020	-0.020	-0.020	-0.020	-0.019	-0.019

605	14.0	590	12.8
685	16.2	555	8.0
725	18.6		
750	18.0	540	6.5
800	16.0	447	0.0
805	15.8		
810	15.6		
815	15.2		
820	14.8		
825	14.5		
834	14.1		
835	13.6		
840	13.2		
845	13.0		
850	12.9		
855	12.8		
860	12.5		
870	12.9		
880	13.3		
890	13.8		
900	14.4		

Density of Clockoil

10/24/11

By R. A. Millikan

Oil & bottle

Rest point 10.9 wt, 20.171 Sins. 2 air pump. Temp 18°C

Bottle alone

Rest point 10.6 wt, 10.9180

Water + Bottle

wt 20.933

→ Temp 18°C

$$\text{wt of oil alone} = \frac{20.171}{10.918} - 1 = 9.253$$

$$\text{Relative wts} = 9.239$$

$$\begin{array}{r} 9.56 \\ 99.91 \\ \hline 196.47 \end{array}$$

$$\text{wt of water alone} = \frac{20.933}{10.918} - 1 = 10.015$$

$$\text{Absolute WT} = 9.239 \times 99.91 = 9.230$$

Determined by S. J. Parralle, 10/31/11.

$$\begin{array}{l} \text{Density at } 14^\circ\text{C} = 0.9252 \\ \text{Density at } 22^\circ\text{C} = 0.9202 \end{array} \quad \therefore \text{Mean change per degree C.} = .000625$$

Note:-

A correction of .0041% per degree C. must be applied for change in viscosity of air. 23°C. is the temp. where no correction is needed. Below 23°, the correction must be subtracted.

A correction of .0004% per degree must be applied for change in density of oil. This correction can be applied with 23° as the point of no correction. It is also minus when the temp. is below 23°. Correction for (change of viscosity + change of density) = .0045% per degree C.

Saturday - 10/28/11.

3:30 P.M. to 4:30

(22.5)

Volts

G

F

$t = 15.8$

$p = 20.51$

840.1 + 13.2
828 + 14.2
818 + 14.9
843 + 13.0
845 + 13.0
837 + 12.9

19.6
19.1
19.4
19.6
19.4
19.6

5011 + 81.2

5092

At Beginning

Lower field

19.4
19.3
19.4
19.3
19.5
19.2
19.6
19.4
19.3

5082

5639

53

Volts

= 5052

Log

3.7035

Weighted mean volts over this period = 5052 Volts

Upper field

19.8
19.4
19.5
19.3
19.7
19.6
19.6

Volts

5039

At End.

7.7157
1.7157
3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

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7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

7.7157

1.7157

3.2157

Drop changed from Neg. to Pos. about middle of observation.

$$V_1 = \frac{5232}{19.484} = 0.02685$$

$$V_1' = \frac{5232}{8.2} = 0.0638$$

$$V_2' = \frac{K}{10.2} = 0.0513$$

$$V_2'' = \frac{K}{14.2} = 0.03685$$

$$V_2''' = \frac{K}{21.08} = 0.02482$$

$$V_2^{IV} = \frac{K}{43.7} = 0.01201$$

$$V_2^{VI} = \frac{K}{52.5} = 0.00997$$

where $K = 5232$

$$\log V_1 + V_2 = 2.1115$$

$$7.2145$$

$$3.1983$$

$$-6.5243$$

$$3.7035$$

$$-10.8208$$

$$\frac{6619}{.214} = 10^{-10}$$

$$6.405 = C$$

$$\log = -10.815$$

Explanation:

(10.2) means

the mean of 1

values of the

2nd speed.

and (43.7) means

the mean of 4 values

of the 5th speed.

$e\%$

l

a

$\frac{l}{a}$

$$-10.8152$$

$$-4.8548$$

$$-16.4327$$

$$-5.5426$$

$$3|-19.6264$$

$$1.3120$$

$$2.4290$$

$$-4.1512$$

$$-7.8755$$

$$-5.5428$$

$$3.7035$$

$$-1.3914$$

$$75.08 \times 10^{-8}$$

$$.0000349$$

$$-14.6652$$

$$.2463$$

$$3|-12.4537$$

$$-4.1512$$

$$.0001417$$

Density of Clockoil

10/24/11

By R. A. Millikan

Oil 48 bottle

Rest point 10.9 wt. 20.171 Sins. 2 div for mg. Temp 18°C

Bottle alone

Rest point 10.6 wt. 10.9180

Water + Bottle

wt 20.933

→ Temp 18°C

$$\text{wt of oil alone} = \frac{20.171}{10.918} = 1.847$$

$$\text{Relative wts} = 0.9239$$

$$\text{wt of water alone} = \frac{20.933}{10.015} = 2.090$$

$$\text{Absolute WT} = 0.9239 \times 99867 = 9230$$

Determined by L. J. Parralle, 10/31/11.

$$\begin{aligned} \text{Density at } 14^\circ\text{C} &= 0.9252 \\ \text{" " } 22^\circ\text{C} &= 0.9202 \end{aligned} \quad \therefore \text{Mean change per degree C.} = .000625$$

Note:-

A correction of .0041% per degree C. must be applied for change in viscosity of air. 23°C. is the temp. where no correction is needed. Below 23°, the correction must be subtracted.

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26

Oct 26

10/29/11 - 4:30 P.M. to 5:40

Positive - Normal Color

At Beginning

Volts

G

F

$\lambda = 16.0$

$f = 21.58$

839 + 13.4
823 + 14.6
813 + 15.4
840 + 13.2
804 + 15.8
834 + 13.6
49 52 + 89.0
97
5039

70 8.7
70 8.9
90 8.6
80 8.6
80 9.0
80 8.4
82 8.6
81 8.7
81 8.8
81 9.0
81 8.8
81 9.0
83 8.3
80 8.9
81 9.0
82 8.7
80 9.0
80 8.8
82 9.0
81 8.9

7.7187
2.9987
5.7710
7.7187
2.9987
5.7710
7.7187
2.9987
5.7710
7.7187
2.9987
5.7710

$$V_1 = \frac{0.5232}{5.722} = 0.09141$$

$$V_2' = \frac{0.5232}{12.55} = 0.04170$$

$$V_2'' = \frac{K}{15.607} = 0.03253$$

$$V_2''' = \frac{K}{28.97} = 0.01806$$

$$V_2^{IV} = \frac{K}{213.0} = 0.002346$$

where $K = .5232$

$$\log K + V_2 = -3.8920$$

$$\frac{1}{2} \log V_1 = -1.3890$$

$$\frac{1}{2} \log V_2 = -3.1983$$

$$-6.4793$$

$$3.7613$$

$$\log e = -10.7180$$

$$C = (5.978 + .159) 10^{-10} = 5.81 \times 10^{-10}$$

$$\log = -10.7842$$

At End

837 + 14.3
821 + 14.7
812 + 15.4
840 + 13.2
780 + 17.0
833 + 13.6
49 33 + 89.9
99
5021

Mean = 8.92

97

Corrected = 8.723

Stepwise
corr

36) 240 (96
234
60

8092

= 1.1% high

eV

-10.7642

3 19.5284

-7.8428

69.68 x 10⁻⁹

l

-4.8547

1.3840

-5.5207

.00003317

3

.0002188

a

-16.4327

-2.7780

3.7613

-14.9120

-3.8920

-11.0200

-4.3400

$\frac{e}{h}$

-5.5207

-4.3400

-1.1807

.1516

(P)

(= 27)

10/29/11 - 5:45 P.M. to 6:20

Red - Positive

$$t = 15.9$$

$p = 22.07$

Volts	G	F
5021	15.2	14.97
at Beginning	15.4	14.92
	14.7	14.85
Weighted	15.1	14.76
Mean Volts	14.9	14.68
4993 Volts	15.1	14.63
	14.9	14.57
	15.2	14.50
log = 3.6984	15.1	14.43
	14.9	14.36
	15.1	14.29
	15.2	14.22
	15.1	14.15
	15.2	14.08
	15.0	14.01
	15.2	13.94
	15.0	13.87
	14.8	13.80
	14.9	13.73
	15.2	13.66
	15.0	13.59
	14.8	13.52
	14.8	13.45
	14.8	13.38
	14.8	13.31
	14.8	13.24
	14.8	13.17
	14.8	13.10
	14.8	13.03
	14.8	12.96
	14.8	12.89
	14.8	12.82
	14.8	12.75
	14.8	12.68
	14.8	12.61
	14.8	12.54
	14.8	12.47
	14.8	12.40
	14.8	12.33
	14.8	12.26
	14.8	12.19
	14.8	12.12
	14.8	12.05
	14.8	11.98
	14.8	11.91
	14.8	11.84
	14.8	11.77
	14.8	11.70
	14.8	11.63
	14.8	11.56
	14.8	11.49
	14.8	11.42
	14.8	11.35
	14.8	11.28
	14.8	11.21
	14.8	11.14
	14.8	11.07
	14.8	11.00
	14.8	10.93
	14.8	10.86
	14.8	10.79
	14.8	10.72
	14.8	10.65
	14.8	10.58
	14.8	10.51
	14.8	10.44
	14.8	10.37
	14.8	10.30
	14.8	10.23
	14.8	10.16
	14.8	10.09
	14.8	10.02
	14.8	9.95
	14.8	9.88
	14.8	9.81
	14.8	9.74
	14.8	9.67
	14.8	9.60
	14.8	9.53
	14.8	9.46
	14.8	9.39
	14.8	9.32
	14.8	9.25
	14.8	9.18
	14.8	9.11
	14.8	9.04
	14.8	8.97
	14.8	8.90
	14.8	8.83
	14.8	8.76
	14.8	8.69
	14.8	8.62
	14.8	8.55
	14.8	8.48
	14.8	8.41
	14.8	8.34
	14.8	8.27
	14.8	8.20
	14.8	8.13
	14.8	8.06
	14.8	7.99
	14.8	7.92
	14.8	7.85
	14.8	7.78
	14.8	7.71
	14.8	7.64
	14.8	7.57
	14.8	7.50
	14.8	7.43
	14.8	7.36
	14.8	7.29
	14.8	7.22
	14.8	7.15
	14.8	7.08
	14.8	7.01
	14.8	6.94
	14.8	6.87
	14.8	6.80
	14.8	6.73
	14.8	6.66
	14.8	6.59
	14.8	6.52
	14.8	6.45
	14.	

$$\begin{array}{r} 1.7187 \\ + 4.0433 \\ \hline 5.7620 \end{array}$$
$$V_1 = \frac{0.5232}{15.011} = 0.03484$$
$$V_2' = \frac{0.5232}{8.75} = 0.0598$$
$$V_2^H = \frac{K}{10.35} = \frac{1.0746}{10.35} = 0.1038$$
$$V_2^{in} = \frac{K}{19.3} = \frac{0.0339}{710.5790}$$
$$V_2^{10} = \frac{K}{19.3} = \frac{0.02951}{0.000345} = 0.0855$$
$$V_2 = \frac{K}{69.17} = 0.00759$$

where $K = 0.9 \times 10^6$

 $\log K_{HCl} = -2.0252$
$$\log V_1 = -1.2911$$
$$\begin{array}{r} -3.1955 \\ \hline \end{array}$$

- 6.4940
6.284

$$\begin{array}{r} 3.6457 \\ \hline 296 \end{array}$$

Q = 10.77

$$e = (6.255 - .203) \cdot 10^{-10}$$
$$6.052 \times 10^{-10}$$
$$\log = -10.7819$$
$$\begin{array}{r} e^{7/3} \\ -10.7519 \\ \hline 3 \overline{) 14.5638} \\ -9.8546 \\ \hline \end{array}$$
$$\begin{array}{r} 2 \\ -4.8542 \\ \underline{1.3441} \\ -5.5101 \end{array}$$
$$\begin{array}{r} -16.4327 \\ -2.5425 \\ \hline 3.6988 \\ -14.6737 \end{array}$$
$$\begin{array}{r} -5.5101 \\ -4.2162 \\ \hline -1.2939 \end{array}$$

Nov 17 / 11

Thomson (Cathode) Fall distance 13.94 mm
Time 21.7

$P = \text{diameter} = 74.0 \text{ cm}$
 $V_1 = \frac{13.94}{22.55} = .6181$

$V_2 = \frac{13.94}{50.3} = .2771$
 $V_3 = \frac{13.94}{34.4} = .4052$

$\frac{1.10233}{.01279}$

Volt

837 + 13.5
818 + 15.0
828 + 14.0
803 + 16.0
774 + 17.3
832 + 13.8

4892 + 89.6
4982

$\log V_1 + V_2 = 3.2069$
 $\frac{1}{2} \log V_1 = 7.3956$
 -3.1943
 $= 4.2013$
 3.6974
 -9.0034

70.54

$8.025(10^{-9})$
 $7.978 \cdot 10^{-9}$

Nov. 18, 1911.

18 small divisions,
starting from 2nd long
division at bottom of field

$t = 18.0^\circ \text{C.}$
 $p = 73.95 \text{ cm.}$

G

F

17.0	5.9		
17.2			
17.1		→ 9.53	$\frac{0.1048}{1.2287}$
16.9	8.6		$\frac{2.5761}{2.5761}$
16.9	9.0		$\frac{2.1048}{2.9460}$
17.1	9.9		$\frac{7.1548}{7.1548}$
	10.3		
	10.1		$\frac{0.1048}{1.0025}$
	10.2		$\frac{1.1023}{1.2148}$
16.8	9.8	10.06	$\frac{1.1023}{1.2148}$
16.9	9.9		$\frac{2.5900}{2.5900}$
16.8	10.2		$\frac{0.1048}{1.4773}$
			$\frac{2.6355}{2.6355}$
17.0			
17.3	16.6		$\frac{0.1048}{1.9360}$
	16.2	16.4	$\frac{2.1655}{2.1655}$
16.8	16.4		$\frac{0.1048}{2.5607}$
16.7			$\frac{3.5441}{3.5441}$
17.0	29.4	29.6	
17.0	29.8		$\frac{0.1048}{2.1436}$
17.0	86.3	46.3	$\frac{3.9812}{3.9812}$
16.8	363.7	363.7	
16.6	139.2	139.2	

$n_{\text{vac}} = 16.93$

Volts

847 + 13.0

837 + 14.5

809 + 15.7

850 + 13.3

838 + 14.5

845 + 13.0

826 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

810 + 13.0

$\log 5110 = 3.7084$

$\frac{12.73}{5110} = 1.273 \text{ cm}$

12.73 = dist between
cross-hairs

$\log 1.273 = 0.1048$

$$V_1 = \frac{1.273}{16.93} = 0.07518$$

$$V_2 = \frac{1.273}{8.83} = 0.14420$$

$$V_2' = \frac{1.273}{10.06} = 0.1266$$

$$V_2'' = \frac{1.273}{16.4} = 0.07762$$

$$V_2''' = \frac{1.273}{29.6} = 0.04300$$

$$V_2^{IV} = \frac{1.273}{86.3} = 0.01475$$

$$V_2^{V} = \frac{1.273}{363.7} = 0.00350$$

$$V_2^{VI} = \frac{1.273}{139.2} = 0.009145$$

$$V_2^{VII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{VIII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{IX} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{X} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XI} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XIII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XIV} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XV} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XVI} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XVII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XVIII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XIX} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XX} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XXI} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XXII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XXIII} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XXIV} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XXV} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XXVI} = \frac{1.273}{437.5} = 0.00291$$

$$V_2^{XXVII} = \frac{1.273}{437.5} = 0.00291$$

weighted
mean = $(V_1 + V_2)$
from each reading
= 0.0056225

$$\log V_1 + V_0 = 3.7449$$

$$\frac{1}{2} \log V_1 = 7.4381$$

$$\log V_0 = 5.1983$$

$$-6.3863$$

$$3.7084$$

$$70.6779$$

Not sure of
distance
1.273

Very low something wrong

Wednes - 11/22/11 → 4:15 P.M.

4:45 P.M.

$$t = 17.5$$

$$\text{dist} = 10.23 \text{ mm}$$

$$p = 75.0$$

Volts	G	F
855 + 13.5	16.2	12.2
849 + 13.2	15.9	12.3
835 + 14.4	16.2	
861 + 12.9	16.0	20.2
854 + 13.5	16.0	100.2
952 + 13.5	16.2	
5106 + 80.0	16.083 = Mean	
80		

$$5186$$

$$\log 5186 = 3.$$

$$V_1 = \frac{1.023}{16.083} = .06362$$

$$V_2 = \frac{1.023}{12.25} = .08352$$

$$V_2' = \frac{1.023}{20.2} = .05065$$

$$V_2'' = \frac{1.023}{100.2} = .01021$$

$$\text{mean} = .006717$$

$$\log V_1 + V_2 = -3.8291$$

$$2.11 V_1 = -1.4018$$

$$3.1963$$

$$-6.4272$$

$$3.7144$$

$$10.7124$$

$$e = 5.158$$

$$5.030$$

11/24/11 → 5:10 P.M.

Volts	G	F
850 + 13.2	35.2	25.7
844 + 13.4	35.4	25.2
827 + 14.0	35.2	49.9
857 + 13.2	35.2	49.8
848 + 13.1	35.4	50.0
846 + 13.1	35.4	147. = 5 small divisions
5072 + 80.0	35.267 = Mean	
80		

$$5157$$

$$\log 5157 = 3.7124$$

$$t = 19.3$$

$$\text{dist} = 10.23$$

$$p = 75.0$$

$$0.0099$$

$$1.3473$$

$$5.4625$$

$$0.0098$$

$$1.3160$$

$$3.6938$$

$$0.0098$$

$$1.4059$$

$$3.6041$$

$$0.0099$$

$$1.6979$$

$$2.3179$$

$$0.0098$$

$$3.3716$$

$$4.6353$$

$$V_1 = \frac{1.023}{35.267} = 0.02901$$

$$V_2 = \frac{1.023}{25.7} = 0.03941$$

$$V_2' = \frac{1.023}{25.45} = 0.04019$$

$$V_2'' = \frac{1.023}{49.867} = 0.02051$$

$$V_2''' = \frac{1.023}{147.16} = 0.00695$$

$$V_2'''' = \frac{1.023}{255.2} = 0.00401$$

$$\log(V_1 + V_2) = 3.9958$$

$$V_2 \log V_1 = 7.3318$$

$$3.1983$$

$$-6.4254$$

$$3.7134$$

$$-16.7130$$

$$e = 5.165$$

$$e = 5.057$$

Thurs - 11/23/11 5:10 P.M.

$$t = 20.8$$

$$P = 75.05$$

Volts	G	F
853 + 135	16.8	15.6 → 15.6
855 + 135	16.8	12.9 → 12.9
829 + 140	17.0	39.12 → 39.03
860 + 135	16.9	53.01
851 + 135	16.6	52.2 } 52.6
852 + 135	17.0	39.01
5100 + 815	16.6	26.01
815	16.8	25.7 } 25.73
51815	16.6	25.51
	16.8	39.01
	16.5	
	17.0	
	16.769	

$$V_1 = \frac{1025}{16.769} = 0.6113$$

$$V_2 = \frac{12.9}{0.6113} = 0.7945$$

$$V_2' = \frac{39.03}{0.6113} = 0.2626$$

$$V_2'' = \frac{52.6}{0.6113} = 0.19485$$

$$V_2''' = \frac{25.73}{0.6113} = 0.3983$$

$$0.6113 \times 0.7945 = 0.4868$$

$$0.6113 \times 0.2626 = 0.16058$$

$$0.6113 \times 0.19485 = 0.11913$$

$$0.6113 \times 0.3983 = 0.2434$$

$$0.4868 + 0.16058 + 0.11913 + 0.2434 = 1.00996$$

$$1.00996 \div 15 = 0.06731$$

$$\text{mean } V_1 + V_2 = 0.06724$$

$$\log V_1 + V_2 = 3.8277$$

$$\frac{1}{2} \log V_1 = 1.9138$$

$$\frac{1}{2} \log V_2 = 1.9138$$

$$\frac{1}{2} \log V_1 + \frac{1}{2} \log V_2 = 3.8277$$

$$\log V_1 + \log V_2 = 7.6554$$

$$\log V_1 + \log V_2 = 7.6554$$

$$\log V_1 + \log V_2 = 7.6554$$

$$e_1 = \frac{5.080}{5.6} = 0.9071$$

$$29.2 \text{ cm}$$

11/23/11 - 5:40 PM.

$\lambda = 21.5$
 $P = 75.05$

Volts at 5:30

	G	F
850+	12.8	
851+	12.8	
820+	12.8	
860+	12.8	
847+	12.8	
849+	12.8	
5077	13.0	
	12.8	
	13.0	12.4
	13.2	

Volts at 6:00

847+	12.9	17.2
845+	13.1	17.4
818+	12.9	24.3
858+	12.9	24.5
843+	12.8	24.3
848+	12.8	
	12.942	
	12.80	

5183.

$$\frac{.0107}{2.360} V_1 = \frac{1025}{12.81} = .08194$$

$$V_2 = \frac{1025}{17.3} = \frac{.05925}{.14129} \div 24 = .005805$$

$$V_3 = \frac{1025}{24.53} = \frac{.04178}{.12372} \div 21 = .005803$$

mean = .005803

$\log V_1 + V_2 = 3.7636$

$\frac{1}{2} V_1 = 1.4518$

$$\begin{array}{r} 31983 \\ - 64137 \\ \hline 37146 \\ - 108996 \\ \hline \end{array}$$

$$\begin{array}{r} 5001 \\ 24 \\ \hline 5240 \\ 4967 \\ \hline \end{array}$$

39.1 cm

Tues. - Nov. 28, 1911

$t = 21.3^{\circ}\text{C.}$

$p = 75$

Volts	G	F
823+14.6	(S) 19.0	
800+16.0	" 19.0	
791+15.6		
827+	(S) 18.8	
797+	" 18.8	
825+	" 18.8	9.0
	" 19.2	45.2
		45.1
		45.2
		45.1

Sat., Dec. 9, 1911.

$$\pm = 24.0$$

$$p_0 = 15.23$$

dist. in between cross-hairs = 1.022 cm.

G F

Volts

(3) 26.6

(5) 26.4

$$838 + 13.4$$

(5) 26.2

11.1

$$840 + 13.2$$

$$826 + 14.4$$

$$853 + 12.8$$

19.8

$$845 + 13.0$$

20.1

$$824 + 14.5$$

(5) 26.2

29.4

$$5026 + 81.3$$

(5) 26.5

$$5107$$

(3) 26.1

56.4

$$\log 5107 =$$

Mean of

6(p.w.) =

26.33

Mean of

5(c) =

26.06

Note.

Manometer has gotten air into it. The correction that must be applied on this account at pressure of 73.63 (on manom.) is + 1.18 cm.

12/4/11

$$t = 24.4$$

$$p = 76.73$$

$$\text{dist} = 10.06$$

Volls

G

F

829 + 14.2

832 + 13.9

795 + 15.8

845 + 13.0

827 + 14.3

818 + 15.0

494.6

86.2

5032.2

22.2

21.8

22.1

22.2

22.0

22.0

22.0

21.848

22.076

21.446

21.460

22.048

22.036

22.060

22.156

22.024

17.2

46.9

151.6

70.6

71.6

71.8

71.4

71.4

152.8

change
slope

$$V_1 = \frac{10.06}{22.024} = .4562$$

$$V_2 = \frac{10.06}{152.7} = .06609$$

$$V_2' = \frac{10.06}{71.36} = .1410$$

$$V_2'' = \frac{10.06}{46.9} = .2144$$

$$V_2''' = \frac{10.06}{196.7} = .05112$$

$$V_2^{(4)} = \frac{10.06}{172} = .05847$$

$$7) 0.5228 \quad 3) 0.5777 \quad 4) 0.6711 \quad 11) 0.9688$$

$$\text{mean } V_1 + V_2 = .007462$$

$$\log V_1 + V_2 = -3.8728$$

$$\log V_1 = -1.3298$$

$$\begin{array}{r} 3.1983 \\ -6.4009 \\ 3.7014 \\ 10.6991 \end{array}$$

$$\begin{array}{r} 5.001 \\ 32 \\ 5.033 \end{array}$$

$$5.033 \text{ which is } 3.2\% \text{ error}$$

$$\begin{array}{r} .0001 \\ 1.3429 \\ 2.6576 \end{array}$$

$$\begin{array}{r} .0001 \\ 2.1824 \\ 3.4201 \end{array}$$

$$\begin{array}{r} .0001 \\ 1.8535 \\ 2.1490 \end{array}$$

$$\begin{array}{r} .0001 \\ 4.715 \\ 2.2215 \end{array}$$

$$\begin{array}{r} .0001 \\ 1.2934 \\ 2.7086 \end{array}$$

$$\begin{array}{r} .0001 \\ 2.255 \\ 2.7670 \end{array}$$

12/3/11

Then 24.25 $\lambda = 75.23$ $d = 102$

G F

~~2650~~

5,300 9,116 c

5,204 9,096 c

5,266

5,274 9,270 c

5,260 9,400 c

5,190

5,268 9,516 c

5,194

5,116

5,198

5,238 20.6 s

5,224 39.69 c

5,350 39.2 SW

5,260

5,186

5,362

$$\left. \begin{array}{l} 44.6 \text{ SW} \\ 45.1 \text{ SW} \\ 45.8 \text{ SW} \\ 45.6 \text{ SW} \end{array} \right\} 45.3$$

5,270

~~5,446~~

19,891.60

5,245

mean 19.

5,192

829 + 14.2

821 + 14.4

803 + 15.9

842 + 13.1

827 + 14.3

816 + 15.1

4948.866

86.6

50346

$$\begin{array}{r} 10094 \\ 0.7154 \\ \hline 7.1437 \end{array}$$

$$V_1 = \frac{10.22}{5.192} = 1.9663$$

$$\begin{array}{r} 10094 \\ 6.61 \\ \hline 3.513 \end{array}$$

$$V_2 = \frac{10.22}{4.55} = 2.246$$

$$\begin{array}{r} 10094 \\ 5.96 \\ \hline 4.924 \end{array}$$

$$V_3 = \frac{10.22}{3.92} = 2.607$$

$$\begin{array}{r} 10094 \\ 4.453 \\ \hline 4.453 \end{array}$$

$$V_4 = \frac{10.22}{3.06} = 3.340$$

$$\begin{array}{r} 10094 \\ 9.671 \\ \hline 10.479 \end{array}$$

$$V_5 = \frac{10.22}{9.28} = 1.101$$

$$3.067 \div 83 = 0.03695$$

$$\text{mean } v_1 + v_2 = 0.0365$$

$$\log v_1 + v_2 = -3.5624$$

$$\frac{1}{2} \log v_1 = -1.6469$$

$$3.1983$$

$$-6.4076$$

$$3.7020$$

$$10.7020$$

$$5.035$$

Unfortunately, this cannot be counted since number is uncertain but must get some of these rapid spectra and chronograph and 10000 volts.

Sat., Dec. 16, 1911.

$$\lambda = 17.5^\circ \text{C.}$$

$$p = 75.14$$

$$\text{dist.} = 1.022 \text{ cm.}$$

Volts	STOP WATCH	STOP WATCH	Chronoscope G	Chronoscope F
844 + 13.0	25.2	32.8	212.86	
847 + 13.0	25.2	26.3	87.45	
823 + 14.6	25.4	26.4	125.41	
850 + 12.9	25.6	33.2		
840 + 13.2		32.9		
673 + 16.3				
4977 + 82.7				
83				
4960				
log 49612				
3.				

Volts	S.W. G	S.W. F	Sat., Dec. 16, 1911	$\lambda = 17.5$
4945	107.4	41.3	dist = 1.022 cm.	$p = 75.4$
log 4945	107.3	41.2		
3.				

Sat., Dec. 16, 1911. dist. = 1.022 cm.

 $t = 17.5^\circ \text{C.}$
 $p = 76.18 \text{ cm.}$

Volts	Stop Watch G	Stop Watch F	Chronoscope G				Chronoscope F		
838 + 13.3	29.9		159.61	268.23	172.52	66.56	222.52	264.69	
839 + 13.3	30.0		10.67	59.61	23.34	8.23	79.58	71.61	
822 + 14.6	30.0		148.94	148.62	149.18	58.33	142.64	193.04	
846 + 13.0	29.9		"	"	"	"	"	"	
854 + 13.7	29.6		29.788	29.729	29.886	"	"	"	
850 + 17.2	29.8		171.61	213.66	162.89	11.666	28.528	38.608	
4949 + 85.0	30.2	38.4	22.52	64.65	13.66				
4934	29.9	28.9	149.09	149.01	149.23				
	29.9	56.9	"	"	"				
	29.6	29.0	29.818	29.802	29.846				
	29.4	38.6	159.67	29.755	29.755				
	29.8	38.9	18.58	29.724	29.724				
		38.8	148.25	29.836	29.836				
		23.2	29.650	29.818	29.802				
		57.8		29.846	29.846				
				24.68	24.68				
				21.08512	21.08512				
				29.650	29.650				
				29.35162	29.35162				
				29.770	29.770				

mean

G. 29.80 29.790
F. 38.675 38.608
T. 28.95 28.52

.0094
34734
-2.5356.0094
5292
-2.4226.0094
7376
-2.504.0094
932
-2.504.0094
3657
-64.34.0094
8672
-1.9424

$$V_1 = \frac{1022}{29.770} = .03433$$

$$V_2 = \frac{1022}{38.67} \cdot \frac{.02650}{.03433} = .06088 \div 7 = .008690$$

$$V_2' = \frac{1022}{57.35} \cdot \frac{.01782}{.03433} = .05215 \div 6 = .008691$$

$$V_2'' = \frac{1022}{28.74} \cdot \frac{.03556}{.03433} = .06989 \div 8 = .008736$$

$$V_2''' = \frac{1022}{23.2} \cdot \frac{.04404}{.03433} = .07637 \div 9 = .008701$$

$$V_2^{(4)} = \frac{1022}{11.66} \cdot \frac{.06758}{.03433} = .12191 \div 5 = .008708$$

$$\text{mean } V_1 + V_2 = .008691$$

$$\log V_1 + V_2 = -3.9341$$

$$\log V_1 = -1.2678$$

$$3.1983$$

$$6.4052$$

$$3.6932$$

$$10.7120$$

$$5152$$

$$128$$

$$5.024$$

This is 4% low.

Mon. - Dec. 18, 1911.

$d =$

$t = 18.0^\circ \text{C.}$

$p = 76.36 \text{ cm.}$

Volts

G

F

847 + 13.6 (S) 37.6 (S) 10.5

846 + 13.0 (S) 37.9

828 + 13.9 (S) 37.8 (S) 10.0

849 + 12.9 (S) 37.9

840 + 13.2 (S) 37.69 (S) 24.2

709 + 16.8 (S) 38.0 (S) 14.48?

(S) 24.0

(S) 24.4

(S) 38.23

(S) 38.2 (S) 24.51

(S) 38.2

(S) 38.2 (S) 46.4

Mon. Dec. 18, 1911

$d =$

$t = 18.0^{\circ} \text{C.}$

$p = 76.83$

G	F
(s) 32.0	(s) 14.9
(s) 32.6	(s) 16.2
(s) 32.2	(s) 19.8
(s) 32.1	(s) 24.9
(s) 32.2	(s) 27.8
(s) 32.6	

1/2
Volly
dropping

Tues. Dec. 19, 1911.

Pos. and reddish

$d =$

$t = 21.0^{\circ} \text{C.}$

$p = 76.13 \text{ cm.}$

G	F
(s) 26.9	Commenced observ. at
(c) 27.34	2:00 P.M.
(s) 27.3	Ended obs. at 2:20
(c) 27.39	
(s) 27.4	
(c) 27.37	(c) 8.07
(s) 27.3	(s) 20.7
(c) 27.35	(s) 31.2
(s) 27.5	(c) 43.17

Volts at
2:00 P.M.

856 + 12.5
855 + 12.5
842 + 12.2
860 + 12.5
852 + 12.9
858 + 12.8

526 + 99.3
77
5203

Volts at
2:20 P.M.

846 + 13.0
848 + 13.0
834 + 13.7
857 + 12.8
849 + 12.9
855 + 12.8
5089 + 73.2
76
5167

Tuesday, Dec. 19, 1911

$d =$

$t = 21.0^{\circ}\text{C.}$

$p = 76.34.$

Readings from 2:40 to 3:00

Volts at	G	F
4:05 P.M.	(S) 31.8	(S) 19.9
	(S) 31.8	
844 + 13.0	(C) 31.56	(S) 14.8
845 + 13.0	(S) 31.6	
829 + 14.2	(C) 31.70 ^(1.56)	(S) 24.4
852 + 12.9		(S) 14.6
843 + 13.1	(C) 31.62	
849 + 13.0	(S) 31.6	(S) 31.6
	(C) 31.53	(S) 44.4
5062 + 79.2	(S) 31.8	(C) 31.54
79		(S) 73.7
5141	(C) 31.76	(S) 44.2
	(S) 31.7	

Tues., Dec 19, 1911

$$d = \frac{F}{F} = 8 \text{ divisions}$$

$$T = 21.6^\circ \text{C.}$$

$$p = 76.46$$

Readings from 3:15 to 3:59 P.M.

- 1st (S) 63.6 = 1 division time
- 2nd (S) 79.2 = 1 division
- 3rd (S) 56.6 = 1 division
- 4th (S) 68.6 = " "
- 5th (S) 44.0 = " "
- 6th (S) 60.0 = " "
- 7th (S) 66.0 = " "
- 8th (S) 66.8 = " "
- 9th (S) 63.0 = " "
- 10th (S) 45.2 = " "
- 11th (S) 46.0 = " "
- 12th (S) 50.8 = " "
- 13th (S) 55.0 = " "
- 14th (S) 58.2 = " "
- 15th (S) 58.0 = " "

$$31.8 = 8 \text{ divisions}$$

$$31.8 = 5 \text{ divisions}$$

- 1st (S) 38.6 = " "
- 2nd (S) 45.0 = " "
- 3rd (S) 49.0 = " "
- 4th (S) 54.6 = " "

This work on carrying down drops was done to see whether there were any possible corrections to the results indicate that there were. Must look more carefully here for the value of ω .

Tues. Dec. 19, 1911

$d =$

$\lambda = 22.5^\circ \text{C.}$

$p = 77.38 \text{ cm.}$

5:55 to 6:12 P.M.

Volts at

G

6:15

(S) 27.4

(S) 27.6

(C) 27.74

(S) 27.6

(S) 27.9

(C) 27.72

(K) 27.85

(C) 27.60

(C) 27.76

(C) 27.76

(C) 27.76

27.76

27.76

27.76

27.76

27.76

27.76

27.76

27.76

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27.76

27.76

27.76

27.76

27.76

27.76

(S) 72.1

(S) 72.2

(S) 45.7

(S) 25.7

13.2 = time 1st
1/2 dist.

S 33.4

17.0 = time 1st
1/2 dist.

$$v_1 = \frac{1022}{27.74} = 0.3684$$

$$v_2 = \frac{1022}{27.15} = 0.3766 - 0.5100 = 0.2055$$

$$v_3 = \frac{1022}{25.7} = 0.3977 - 0.7001 = 0.0976$$

$$v_4 = \frac{1022}{33.4} = 0.3060 - 0.6744 = 0.0316$$

$$v_5 = \frac{1022}{45.7} = 0.2236 - 0.5920 = 0.0316$$

$$\text{Mean } v_1, v_2 = 0.0316$$

$$\text{Mean } v_1, v_2 = 0.0316$$

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$$\text{Mean } v_1, v_2 = 0.0316$$

$$\text{Mean } v_1, v_2 = 0.0316$$

about 3% low.

Wednesday, Dec. 20, 1911. $\left\{ \begin{array}{l} d = \\ \tau = 22.0^\circ \text{C.} \\ p = 76.9 \end{array} \right.$

Volts at
3:15 P.M. $\left\{ \begin{array}{l} \text{obs. from} \\ 3:30 \text{ to } 3:45 \text{ P.M.} \end{array} \right.$

G F
 $\begin{array}{l} 852 + 12.9 \\ 853 + 12.9 \\ 839 + 13.2 \\ 859 + 12.8 \\ 548 + 12.9 \\ 857 + 12.8 \end{array} \left\{ \begin{array}{l} (29.8 \\ 14.6 \\ 29.8 \\ 14.9 \\ 29.8 \\ 14.9 \end{array} \right. \left\{ \begin{array}{l} \text{at } 1/2 \text{ dist.} \\ \text{at } 1/2 \text{ dist.} \\ \text{at } 1/2 \text{ dist.} \\ \text{at } 1/2 \text{ dist.} \\ \text{at } 1/2 \text{ dist.} \\ \text{at } 1/2 \text{ dist.} \end{array} \right. \left\{ \begin{array}{l} (7.4 \\ 11.3 \end{array} \right.$

Volts at
3:50 P.M. $\left\{ \begin{array}{l} (29.6 \\ 14.6 = 100\% \text{ dist.} \end{array} \right.$
 $\begin{array}{l} 849.5 + 12.9 \\ 851.5 + 12.9 \\ 826 + 14.5 \\ 855 + 12.8 \\ 844 + 13.0 \\ 854 + 12.8 \end{array} \left\{ \begin{array}{l} (30.2 \\ 15.2 = 100\% \text{ dist.} \end{array} \right.$
 $\begin{array}{l} 5080 + 77.5 \\ 76 \\ 5156 \end{array}$
 $\begin{array}{l} 849.5 + 12.9 \\ 851.5 + 12.9 \\ 826 + 14.5 \\ 855 + 12.8 \\ 844 + 13.0 \\ 854 + 12.8 \end{array} \left\{ \begin{array}{l} (29.84 \\ 29.89 \end{array} \right.$
 $\begin{array}{l} 5080.0 + 78.9 \\ 79 \\ 5159 \end{array}$

$$\begin{aligned} v_1 &= \frac{102.2}{29.86} = 0.03422 \\ v_2 &= \frac{102.2}{101.6} = 0.1006 \\ v_1 + v_2 &= 0.4428 \div 5 = 0.08856 \\ \log v_1 + v_2 &= 3.9472 \\ \log v_1 &= 1.2672 \\ &3.1983 \\ &6.4127 \\ &3.7126 \\ &10.7001 \\ &5013 \\ &22 \\ &4991 \end{aligned}$$

Conditions observed particularly good & results should be more than usually reliable. We kept temperature constant within a fraction of a degree in room 12 but found

particularly to be quite constant

Wednes. Dec. 20, 1911. $d =$

$t = 22.2^\circ$

100. drop.
Volts at

Obs. taken from 4:10 to 4:30 P.M.
G F

$p = 78.03 \text{ cm.}$

4:30 P.M.

(S) 14.0

(S) 29.2 (at top of field)

847 + 13.0

849 + 12.9

820 + 14.8

852 + 12.9

841 + 13.2

851 + 12.9

(S) 14.0
7.0 = $\frac{1}{2}$ in

(C) 14.11

(C) 14.28

5060 + 99.7

5140

(C) 14.11

(C) 14.13

(C) 14.02

(C) 14.00

(C) 14.18

(C) 13.95

(C) 13.89

11 154 59
14.05

14.4
13.9
13.5
13.0
12.5
12.0
11.5
11.0
10.5
10.0
9.5
9.0
8.5
8.0
7.5
7.0
6.5
6.0
5.5
5.0
4.5
4.0
3.5
3.0
2.5
2.0
1.5
1.0
0.5
0.0

(S) 24.2

(S) 24.6 24.5

(S) 24.7

(S) 24.6

(S) 43.6

(S) 44.4 17.87
44.68

(S) 45.1

(S) 45.6

(S) 102.6

(S) 104.0 104

(S) 104.0

(S) 105.8
52.4 = $\frac{1}{2}$ in

$$\frac{0.044}{14.28} = \frac{1022}{14.05} = 0.7274$$

$$\frac{0.044}{14.28} = \frac{1022}{14.11} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.13} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.02} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.00} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.18} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{13.95} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{13.89} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.05} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.11} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.13} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.02} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.00} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{14.18} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{13.95} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

$$\frac{0.044}{14.28} = \frac{1022}{13.89} = 0.7274 \rightarrow 0.8256 \div 13 = 0.06351$$

This is a good def.
and is high

Wednes., Dec. 20, 1911 { d =

$$t = 22.3^{\circ}\text{C},$$

$$p = 78.23\text{ cm.}$$

obs. from 4:45 to 5:30 P.M.

Volts at
5:30 P.M.
$$\begin{array}{r} 841 + 13.2 \\ 844 + 13.0 \\ 817 + 15.0 \\ 851 + 12.9 \\ 840 + 13.2 \\ 850 + 12.9 \\ \hline 5043 \quad 60.2 \\ \text{res} \\ \hline 51222 \end{array}$$

G F
 (5) $\begin{cases} 98.0 \\ 42.3 = 1^{st} \text{ half} \end{cases}$ (5) 29.7
 (5) $\begin{cases} 51.5 \\ 26.0 = 1^{st} \frac{1}{2} \text{ div.} \end{cases}$
 ← (5) $\begin{cases} 97.4 \\ 49.0 = 1^{st} \frac{1}{2} \text{ div.} \end{cases}$

(5) $\frac{28.7}{14.6} = 1.96 \approx \frac{1}{2}$ dist.

(3) $\begin{cases} 96.2 \\ 49.0 + 1.5 \\ \hline \end{cases} \frac{1}{2} \text{ dist.} \quad (5) \begin{cases} 51.0 \\ 26.0 = 1.25 \\ \hline \end{cases} \frac{1}{2} \text{ dist.}$

(5) $\begin{cases} 96.2 \\ 48.7 = 1\frac{1}{2}\% \text{ dia} \end{cases} (s) 227.5$

(5) $\begin{cases} 95.5 \\ 49.0 = 1.95 \end{cases}$ % dist. (5) $\begin{cases} 29.0 \\ 14.8 = 1.95 \end{cases}$ % dist.

(5) $\begin{cases} 93.0 \\ 44.0 = 100\% \text{ dist.} \end{cases} \quad \begin{cases} 232 \\ 106.0 = \text{rat. } \frac{1}{2} \text{ dist.} \end{cases} \quad \left. \begin{array}{l} \text{in upper} \\ \text{portion} \\ \text{of field.} \end{array} \right\}$

right in middle of field. (5) $\left\{ \begin{array}{l} 92.0 \\ 46.0 \end{array} \right. \frac{1}{2} \text{ 1st 1/2nd}$

Handwritten calculations for the sum of the first 10 terms of the arithmetic sequence:

$$\begin{array}{r}
 97 \\
 93.0 \\
 96.7 \\
 96.2 \\
 96.2 \\
 95.5 \\
 93.0 \\
 90.0 \\
 86.0 \\
 81.0 \\
 \hline
 855.0
 \end{array}$$

Additional handwritten calculations on the right side of the page:

$$\begin{array}{r}
 .0094 \\
 -6.9736 \\
 \hline
 -6.9642
 \end{array}$$

$$v_1 = \frac{1212}{9495} = 0.1277$$

$$r_2 = \frac{1032}{51.60} = 0.19806 - \frac{0.3058}{2} = 0.1524$$

$$v_2' = \frac{1021}{2271} = 0.4492 - 0.1510 = 0.2982$$

$$K_2 = \frac{1622}{974} = 0.1049$$

$$r_{p,10} = \frac{1000}{2913} = 0.3435$$

MEAN V. 442 = 0.5296

$$\begin{array}{r} \log 4000 = 2.1834 \\ \log 41 = 1.6159 \\ \hline 3.7993 \\ - 6.3981 \\ \hline 2.7092 \\ - 23.6442 \end{array}$$

$Q = 4.98$ which means that there could not have been an oil drop.

Thursday Jan. 4, 1912.

Volts

1 -	857 + 12.8 =	869.8
2 -	862 + 12.8 =	874.8
3 -	823 663 + 15.6 =	678.6
4 -	862 + 12.8 =	874.8
5 -	853 + 12.8 =	865.8
6 -	860 + 12.8 =	872.8
	4957 + 79.6	5036.6

79.6
5036.6

$t = 17.2$ $p = 7401$ (1)

- 21.60 (S)
- 21.53 (C)
- 21.80 (S)
- 21.51 C
- 21.80 S
- 21.68

- 13.46 (C)
- 14.15 (C)

2262 (C)

46.2 (S)

21.71 (C)

46. (S)

21.77 (C)

45.8 (S)

21.57 (C)

46.0 (S)

21.63

$t = 17.2$ $p = 7401$
volts

1 -	853 + 12.8 =	865.8
2 -	847 + 13.1 =	860.0
3 -	825 + 14.5 =	839.5
4 -	855 + 12.8 =	867.8
5 -	842 + 13.1 =	855.1
6 -	854 + 12.8 =	866.8
	5076 + 79.0 =	5155.0
	79	5155

0094
3351
6743

$$V_1 = \frac{1022}{21.63} = 0.4724$$

$$V_2 = \frac{1022}{46.0} = \frac{0.0222}{0.4724} = 0.04724$$

$$\sum V_1 + V_2 = -2.8418$$

$$\frac{1}{2} \sum V_1 = -1.3374$$

$$\frac{1}{2} \sum V_2 = -3.1783$$

$$\frac{1}{2} \sum V_3 = 5.3773$$

$$\frac{1}{2} \sum V_4 = 3.7122$$

$$\frac{1}{2} \sum V_5 = 9.6651$$

46.25
122

$$9 \overline{) 45.03}$$

$$e_1 = 5.003$$

3' 29. low

$$t = 17.4$$

$$P =$$

Volts

$$\begin{aligned} 1 - 849 + 12.9 &= 861.9 \\ 2 - 844 + 13.0 &= 857.0 \\ 3 - 820 + 14.8 &= 834.8 \\ 4 - 850 + 12.9 &= 862.9 \\ 5 - 834 + 13.6 &= 847.6 \\ 6 - 851 + 12.9 &= 863.9 \end{aligned}$$

$$\begin{array}{r} \text{Volts} \\ 5048 + 80.1 = 5128.1 \\ \hline 801 \\ \hline 51281 \end{array}$$

$$17.2 \text{ (S)}$$

$$17.07 \text{ (S)}$$

$$17.3 \text{ (S)}$$

$$17.51 \text{ (S)}$$

$$17.48 \text{ (S)}$$

$$17.46 \text{ (S)}$$

$$17.49 \text{ (S)}$$

$$17.46 \text{ (S)}$$

$$17.50 \text{ (S)}$$

$$17.47 \text{ (S)}$$

$$17.39 \text{ (S)}$$

$$\begin{array}{r} 13976 \\ \times 17.47 \\ \hline \end{array}$$

$$14.99 \text{ (S)}$$

$$42.7 \text{ (S)}$$

$$42.4 \text{ (S)}$$

$$32.7 \text{ (S)}$$

$$33.0 \text{ (S)}$$

$$32.8 \text{ (S)}$$

$$42.4 \text{ (S)}$$

$$42.0 \text{ (S)}$$

$$42.6 \text{ (S)}$$

$$10.1.0 \text{ (S)}$$

$$\begin{array}{r} .0044 \\ 1.242 \\ \times 17.47 \\ \hline 2.1670 \end{array} \quad V_1 = \frac{1022}{17.47} = .05850$$

$$V_2 = \frac{1022}{101.2} = .01011 = .06861 \div 10 = .006861$$

$$\begin{array}{r} .0044 \\ 1.242 \\ \times 17.47 \\ \hline 2.1670 \end{array} \quad V_2' = \frac{1022}{42.82} = .02410 = .08260 \div 12 = .006883$$

$$V_2'' = \frac{1022}{32.83} = .03113 = .08964 \div 13 = .006895$$

$$V_1 + V_2 = .006880$$

$$\log V_1 + V_2 = 3.8376$$

$$\log V_1 = 1.3836$$

$$3.1483$$

$$6.4195$$

$$7100$$

$$7095$$

$$5.122$$

$$12.45$$

$$e_1 = 49935$$

which is 39, low

Thursday Jan. 11th 1912. New Menometer

$t = 19.1$

$t = 19.2$

Volts-

1 - 858 + 12.8 = 870.8
2 - 859 + 12.8 = 871.2
3 - 842 + 13.1 = 855.1
4 - 863 + 13.0 = 876.0
5 - 851 + 12.9 = 863.9
6 - 857 + 12.8 = 869.8

5130 + 77.4 = 5207.4
77.4
5207.4

@ 2:15

@ 12:05

1 - 851 + 12.9 = 863.9
2 - 852 + 12.9 = 864.9
3 - 838 + 13.4 = 851.4
4 - 853 + 12.8 = 865.8
5 - 849 + 12.9 = 861.9
6 - 847 + 12.9 = 859.9

5090 + 77.8 = 5167.8
77.8
5167.8

Obs. taken at 3:25 P.M. $t = 19.4$

$P = 76.61$ (no correction - New menometer)

valts at 4:00 P.M.

65.3 12.8

32.2 } $\frac{1}{2}$ 21.6
65.1 }

32.2 } $\frac{1}{2}$
65.1 }

32.2 } $\frac{1}{2}$ 31.8
64.9 }

31.7 } $\frac{1}{2}$ 31.7
64.7 }

32.6 } $\frac{1}{2}$
64.8 }

32.0 } $\frac{1}{2}$
64.8 }

64.0

16.4 } $\frac{1}{2}$

63.8

31.3 } $\frac{1}{2}$ 16.0 } $\frac{1}{2}$
63.2 }

62.8 32.6

31.6 21.2
63.1

Obs. finished at 3:55

2nd obs. starts @ H:10 $v = 19.4$ P. 76.90

vals at 4:00

$$1 = 846 + 13.0 = 859$$

$$2 = 846 + 13.0 = 859$$

$$3 = 819 + 14.9 = 833.9$$

$$4 = 852 + 12.9 = 864.9$$

$$5 = 834 + 13.5 = 847.5$$

$$6 = 843 + 13.1 = 856.1$$

$$g \quad 5140 + 80.4 = 5120.4$$

16.6-S

16.38-C

16.4-S

16.3-S

16.49-C

16.39-C

16.49-C

16.6-S

16.41-C

16.5-C

14.00-S

15.80-S

16.60-C

31.20-S

16.50-C

25.20-S

16.45-C

3rd Obs. starts at 4:38 $t = 19.5$ $P = 77.16$

Volts at 4:30.

Volts at 4:55.

$$1 - 844 + 13.0 = 857.0$$

$$2 - 845 + 13.0 = 858.0$$

$$3 - 816 + 15.1 = 831.1$$

$$4 - 851 + 12.9 = 863.9$$

$$5 - 833 + 13.8 = 846.8$$

$$6 - 843 + 13.1 = 856.1$$

$$5032 + 80.9 = 5112.9$$

$$\begin{array}{r} 80.9 \\ 5112.9 \end{array}$$

$$1 - 843 + 13.1 = 856.1$$

$$2 - 843 + 13.1 = 856.1$$

$$3 - 815 + 15.2 = 830.2$$

$$4 - 850 + 12.9 = 862.9$$

$$5 - 834 + 13.6 = 847.6$$

$$6 - 841 + 13.2 = 854.2$$

$$5046 + 81.1 = 5127.1$$

$$\begin{array}{r} 81.1 \\ 5127.1 \end{array}$$

G	F
26.6 - 5	84.8 S
	24.2 S
26.45 - 2	45.8 S
26.35 - 2	45.9 S
26.31 - 2	41.9 S
26.30 - 0	84.4 S

Finished at 4:53

4th Obs. starts at 5:10

t=19.5

P=78.05

34

Volts taken @ 4:55 see last page

B.	F
13.67	
13.71	
13.65	c
13.71	c
13.83	c
13.76	c
13.70	s
13.71	c
13.70	c
13.82	c
	22.9 - s
	22.6 - s
	26.2 - s
	26.3 - s
	26.0 - s
13.75	c
	68.0 - s
13.71	c
	49.1 - s
13.77	c

$$V_1 = \frac{1022}{1374} \cdot 0.7438$$

when volts = 50.98

$$V_2 = \frac{1022}{68.0} \cdot \frac{0.1503}{7438} = 0.8441 \div 15 = 0.05627$$

$$V_3 = \frac{1022}{49.1} \cdot \frac{0.2082}{7438} = 0.9520 \div 16 = 0.05950$$

$$V_4 = \frac{1022}{26.7} \cdot \frac{0.3405}{7438} = 1.1343 \div 19 = 0.05970$$

$$V_5 = \frac{1022}{22.6} \cdot \frac{0.4442}{7438} = 1.1920 \div 20 = 0.05960$$

$$V_1 + V_2 = 0.05960$$

$$\log V_1 + V_2 = -3.7752$$

$$\log V_3 = -1.4357$$

$$\log V_4 = -3.1483$$

$$\log V_5 = -3.7074$$

$$\log V_6 = -3.7074$$

$$\log V_7 = -3.7074$$

$$\log V_8 = -3.7074$$

$$\log V_9 = -3.7074$$

$$\log V_{10} = -3.7074$$

$$\log V_{11} = -3.7074$$

$$\log V_{12} = -3.7074$$

$$\log V_{13} = -3.7074$$

$$\log V_{14} = -3.7074$$

$$\log V_{15} = -3.7074$$

$$\log V_{16} = -3.7074$$

$$\frac{16487}{13.74} = 1200$$

finished @ 5:45

Volts taken again - see next page.

which is nearly 4% error

$$\frac{10045}{2} = 5022.5$$

5th Obs. @ 6:05

 $t = 19.6$ $P = 78.4$

Volts at 5:45

- 1- $842 + 13.1 = 855.1$
- 2- $839 + 13.2 = 852.2$
- 3- $810 + 15.6 = 825.6$
- 4- $850 + 12.9 = 862.9$
- 5- $833 + 13.9 = 846.9$
- 6- $839 + 13.2 = 852.2$

$$\begin{array}{r} 5013 \\ 81.9 \\ \hline 5094.9 \end{array}$$

Volts at 6:35

- 1- $836 + 13.6 = 849.6$
- 2- $831 + 14.0 = 845.0$
- 3- $808 + 15.7 = 823.7$
- 4- $845 + 13.0 = 858.0$
- 5- $832 + 13.9 = 845.9$
- 6- $839 + 13.2 = 852.2$

$$\begin{array}{r} 4991 \\ 83.4 \\ \hline 5074.4 \end{array}$$

$$\begin{array}{r} 95.9 \\ 17.5 \\ \hline 78.4 \end{array}$$

b.	F
74.7 } $= \frac{1}{2}$ S	27.8 S
152.4 } (77.7)	
73.0 } $= \frac{1}{2}$ S	-33.6 } $= \frac{1}{2}$ S
149.8 } (76.8)	67.4 } (33.8) S
73.4 } $= \frac{1}{2}$ S	34.6 } $= \frac{1}{2}$ S
149.3 } (75.8)	68.6 } (34) S
75.3 } $= \frac{1}{2}$ S	14.0 } $= \frac{1}{2}$ S
151.6 } (76.3)	27.8 } (13.8) S
74.0 } $= \frac{1}{2}$ S	74.3 } $= \frac{1}{2}$ S
151.0 } (75.8)	27.8 } (13.5) S
73.6 } $= \frac{1}{2}$ S	33.6 } $= \frac{1}{2}$ S
149.8 } (76.2)	68.1 } (34.5) S
74.3 } $= \frac{1}{2}$ S	
149.8 } (75.5)	

$$\begin{array}{r} 74.7 \\ 73.0 \\ 152.4 \\ 73.4 \\ 149.3 \\ 75.3 \\ 151.6 \\ 74.0 \\ 151.0 \\ 73.6 \\ 149.8 \\ 74.3 \\ 149.8 \\ \hline 10537 \\ 150.5 \end{array}$$

$$V_1 = \frac{1022}{150.5} = 6.790626$$

$$V_2 = \frac{1022}{68.03} = 15.023 = 0.2187$$

$$V_3 = \frac{1022}{27.8} = 36.76 = 0.4240$$

$$V_1 + V_2 = 0.2178$$

$$\log V_1 + V_2 = -2.3381$$

$$\log V_1 = -2.9110$$

$$3.1983$$

$$6.4474$$

$$3.7054$$

$$-10.7430$$

$$e = 5.521$$

$$84$$

$$5.437$$

which is 4.57% low

Friday, Jan. 12th 1912Volts taken at 4:15 P.M. $t = 20.5$ $p = 76.3$

- 1- $850 + 12.9 = 862.9$
 2- $855 + 12.8 = 867.8$
 3- $838 + 13.4 = 851.4$
 4- $858 + 12.8 = 870.8$
 5- $852 + 12.9 = 864.9$
 6- $854 + 12.8 = 866.8$

$$5107 + 77.6 = 5184.6$$

$$\frac{5184.6}{77.6}$$

$$\frac{5184.6}{77.6}$$

$$25.4 -$$

$$25.2 -$$

$$25.196$$

$$25.2 -$$

$$25.166$$

$$25.022$$

$$25.264$$

$$25.0 -$$

F

$$39.6$$

$$29.7$$

$$23.8$$

$$24.0$$

$$22.9$$

$$V_1 = \frac{10.22}{25.162} = .40015$$

$$V_2 = \frac{10.22}{39.6} = .25808$$

$$V_3 = \frac{10.22}{29.7} = .3441$$

$$V_4 = \frac{10.22}{23.8} = .4296$$

$$V_5 = \frac{10.22}{24.0} = .4258$$

$$V_6 = \frac{10.22}{22.9} = .4463$$

$$V_7 = \frac{10.22}{25.0} = .4088$$

$$V_8 = \frac{10.22}{25.196} = .4059$$

$$V_9 = \frac{10.22}{25.264} = .4046$$

$$V_{10} = \frac{10.22}{25.0} = .4088$$

$$V_{11} = \frac{10.22}{25.166} = .4065$$

$$V_{12} = \frac{10.22}{25.022} = .4085$$

$$V_{13} = \frac{10.22}{25.162} = .4065$$

$$V_{14} = \frac{10.22}{25.0} = .4088$$

$$V_{15} = \frac{10.22}{25.196} = .4059$$

$$V_{16} = \frac{10.22}{25.264} = .4046$$

$$V_{17} = \frac{10.22}{25.0} = .4088$$

Finish @ 4:35

$$25.196$$

$$25.166$$

$$25.022$$

$$25.264$$

$$100.648$$

$$25.162$$

mean value
= 5172.7

$$\log V_1 + V_2 = 3.91657$$

$$\frac{1}{2} \log V_1 = -1.30105$$

$$-3.19220$$

$$-6.41627$$

$$3.71488$$

$$.70284$$

$$5029$$

$$55$$

$$e = 4.974$$

170 low

3rd Obs.

Volts at 5:30 P.M.

$$\begin{aligned}
 1 - 846 + 13.0 &= 859.0 \\
 2 - 851 + 12.9 &= 863.9 \\
 3 - 828 + 14.3 &= 842.3 \\
 4 - 853 + 12.8 &= 865.8 \\
 5 - 845 + 13.0 &= 858.0 \\
 6 - 847 + 12.9 &= 859.9 \\
 \hline
 5070 + 78.9 &= 5148.9 \\
 \hline
 5148.9
 \end{aligned}$$

t = 20, p = 7.635
Volts taken at 6:05

$$\begin{aligned}
 1 - 846 + 13.0 &= 859.0 \\
 2 - 850 + 12.9 &= 862.9 \\
 3 - 827 + 14.4 &= 841.4 \\
 4 - 853 + 12.9 &= 865.9 \\
 5 - 844 + 13.0 &= 857.0 \\
 6 - 847 + 12.9 &= 859.9 \\
 \hline
 5067 + 79.1 &= 5146.1 \\
 \hline
 5146.1
 \end{aligned}$$

S.	F	
18.912		
18.932		
18.868		
19.052		
18.980	19.5 (S)	19.33
18.964	19.2 (S)	
18.976	17.0 (S)	17.07
19.108	17.1 (S)	
18.984	17.1 (S)	
18.912	19.3 (S)	42.2
18.990	42.2 (S)	
4570	42.2 (S)	
18.957	101.9 (S)	
6.03 p.m.		

$$V_1 = \frac{1022}{18.957} = .005391$$

$$\begin{aligned}
 &.00945 \\
 &1.27777 \\
 &\hline
 &2.73162 \\
 &-1.36569 \\
 &\hline
 &1.36593
 \end{aligned}$$

$$V_2' = \frac{1022}{17.07} = .05987$$

$$\begin{aligned}
 &.00945 \\
 &1.27777 \\
 &\hline
 &2.73162 \\
 &-1.36593 \\
 &\hline
 &1.36569
 \end{aligned}$$

$$V_3'' = \frac{1022}{19.33} = .05287$$

$$\begin{aligned}
 &.00945 \\
 &1.27777 \\
 &\hline
 &2.73162 \\
 &-1.36569 \\
 &\hline
 &1.36593
 \end{aligned}$$

$$V_4''' = \frac{1022}{42.2} = .02422$$

$$\begin{aligned}
 &.00945 \\
 &1.27777 \\
 &\hline
 &2.73162 \\
 &-1.36569 \\
 &\hline
 &1.36593
 \end{aligned}$$

$$V_5^{IV} = \frac{1022}{101.9} = .01003$$

$$\begin{aligned}
 &.00945 \\
 &1.27777 \\
 &\hline
 &2.73162 \\
 &-1.36569 \\
 &\hline
 &1.36593
 \end{aligned}$$

$$V_1' + V_2' = \frac{.05391}{.11378} \div 16 = .002994, .007111$$

$$V_2' + V_3'' = \frac{.05287}{.10678} \div 15 = .002994, .007118$$

$$V_3'' + V_4''' = \frac{.05241}{.107813} \div 14 = .003005, .007103$$

$$V_4''' + V_5^{IV} = \frac{.05241}{.10103} \div 11 = .002244, .007104$$

$$V_5^{IV} + V_1 = \frac{.05241}{.106894} \div 10 = .002244, .007109$$

$$85181 \cdot V_1' + V_2' = .003009$$

$$\text{volts} = 5148$$

$$\begin{aligned}
 \log(V_1 + V_2) &= 47842 \\
 \log V_1 &= 26564 \\
 &19830 \\
 &\hline
 &6.04256 \\
 &2.71164 \\
 &\hline
 &46595 \\
 &21164 \\
 &\hline
 &67759
 \end{aligned}$$

$$\begin{aligned}
 &5062 \\
 &68 \\
 &\hline
 e = 4994
 \end{aligned}$$

Saturday Jan 20, 1911.

Magnification 1005.

Volts at 2:45

t = 23.

P = 9563 - 1754 = 7709

$$\begin{aligned}
 1 - 869 + 12.9 &= 881.9 \\
 2 - 872 + 12.0 &= 885.0 \\
 3 - 860 + 12.8 &= 872.8 \\
 4 - 876 + 12.1 &= 889.1 \\
 5 - 855 + 12.8 &= 867.8 \\
 6 - 870 + 12.9 &= 882.9 \\
 \hline
 5202 + 77.5 &= 5279.5 \\
 77.5 \\
 \hline
 5279.5
 \end{aligned}$$

Volts at 3:50 P.M.

$$\begin{aligned}
 17 \quad 1 - 852 + 12.9 &= 864.9 \\
 16 \quad 2 - 826 + 14.5 &= 840.5 \\
 15 \quad 3 - 845 + 13.0 &= 858.0 \\
 14 \quad 4 - 863 + 12.9 &= 875.9 \\
 10 \quad 5 - 845 + 13.0 &= 858.0 \\
 12 \quad 6 - 858 + 12.8 &= 870.8 \\
 \hline
 5089 + 79.1 &= 5168.1 \\
 79.1 \\
 \hline
 5168.1
 \end{aligned}$$

$$\begin{aligned}
 5279.5 \\
 5168.1 \\
 \hline
 111.4
 \end{aligned}$$

Obs. begun at 3:13 P.M.

G	F
25.2	27.8
	27.8
	19.2
25.558	
25.2	52.4
25.494	
	91.7
25.8	
25.566	91.5
	{ 46.3 = 1/2
25.278	{ 92.4
	{ 46.6 = 1/2
25.260	{ 93.4
	{ 47.
25.564	{ 94.
25.382	93.4
	47.275
25.394	94.4
3.496	
25.462	
3:48	

$$\begin{aligned}
 V_1 &= \frac{1005}{25.462} = .03947 \\
 V_2 &= \frac{1005}{19.2} = .05234 \\
 V_3 &= \frac{1005}{27.8} = .03615 \\
 V_4 &= \frac{1005}{52.4} = .01918 \\
 V_5 &= \frac{1005}{91.5} = .01093 \\
 V_6 &= \frac{1005}{93.4} = .01065
 \end{aligned}$$

$$V_1 + V_2 = .09181 \div 11 = .00835$$

$$= .0756259 \div 7 = .00835$$

$$= .05865 \div 7 = .00838$$

$$E = .050355 \div 6 = .00839$$

$$L(V_1 + V_2) = 920123 - 3$$

$$L \log n = \frac{298137 - 1}{19410 - 3}$$

$$L \log 5200 = \frac{416350 - 1}{71600 - 3}$$

$$L = .50182$$